

- [54] **PSEUDO-RANDOM POINT SAMPLING TECHNIQUES IN COMPUTER GRAPHICS**
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- [52] **U.S. Cl.** 364/522; 340/725; 340/728; 340/729; 364/521
- [58] **Field of Search** 364/518, 521, 522; 340/725, 728, 729, 747

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[57] **ABSTRACT**

A computer database contains visual and other information of an object scene from which a television monitor or film display is created by electronically sampling points of the object scene information in the computer memory. Undesirable effects of aliasing are significantly reduced and substantially eliminated by pseudo-randomly distributing, in a particular manner, the occurrence of the point samples in space and time. Realistic depth of field is obtained in the images, corresponding to what is observed through a camera lens, by altering the sample point locations to simulate passing them through an optical aperture in a pseudo-random distribution thereacross. Further, effects of illumination, shadows, object reflection and object refraction are made more realistic by causing each sample point to pseudo-randomly select one of a predetermined number of possible ray directions.

54 Claims, 4 Drawing Sheets

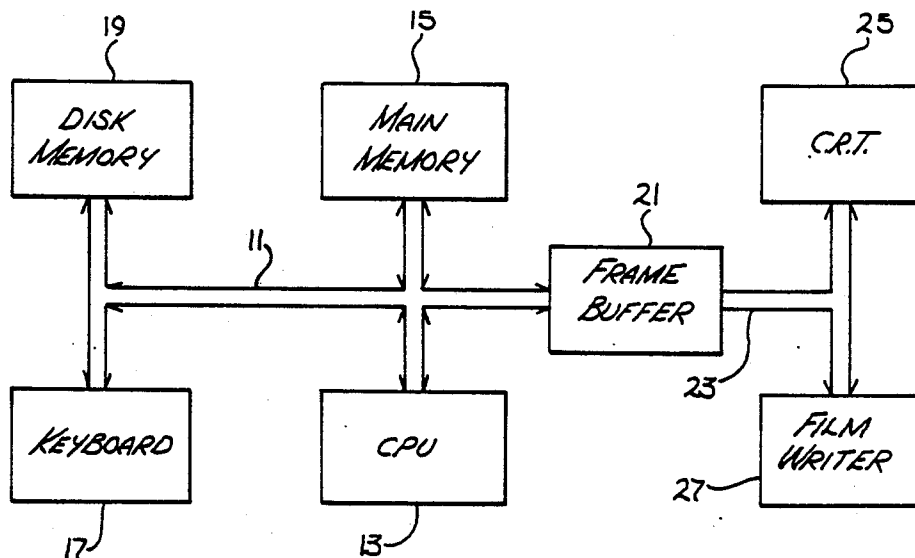


Fig. 1

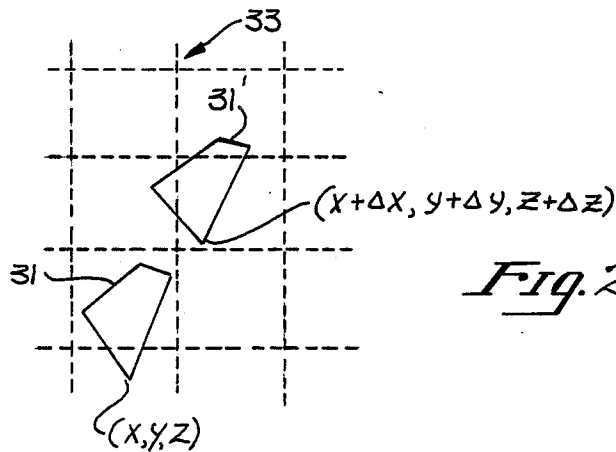
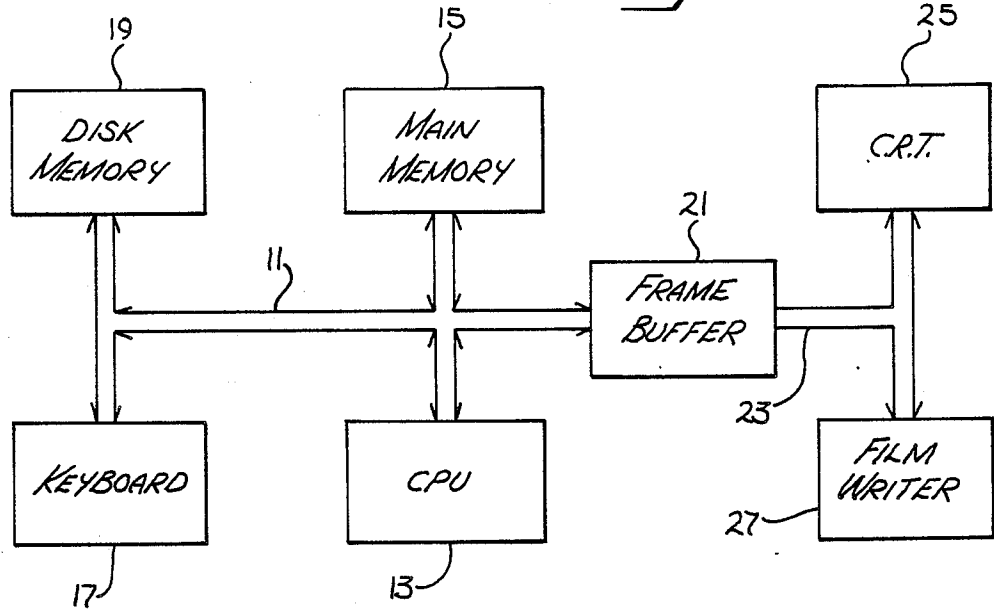


Fig. 2

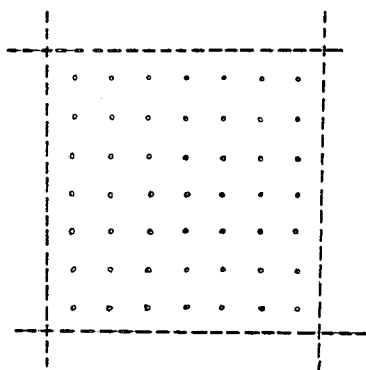


Fig. 3
PRIOR ART

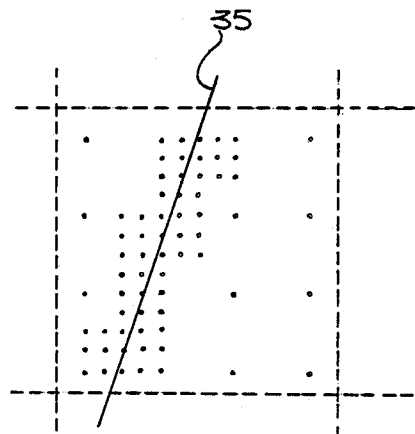


Fig. 4
PRIOR ART

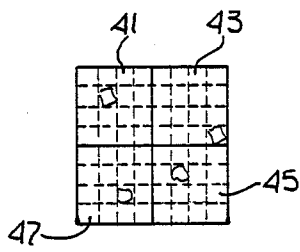


Fig. 5

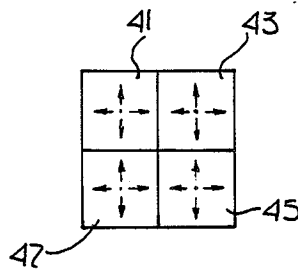


Fig. 6

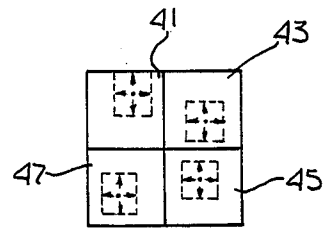


Fig. 7

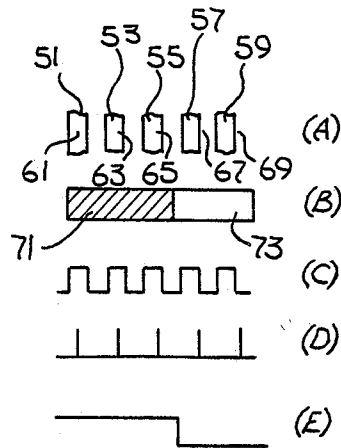


Fig. 8

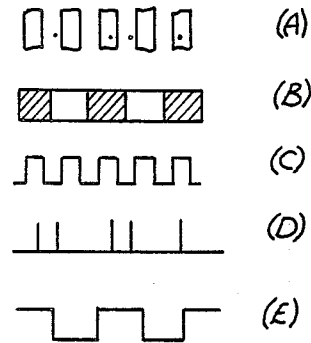


Fig. 9

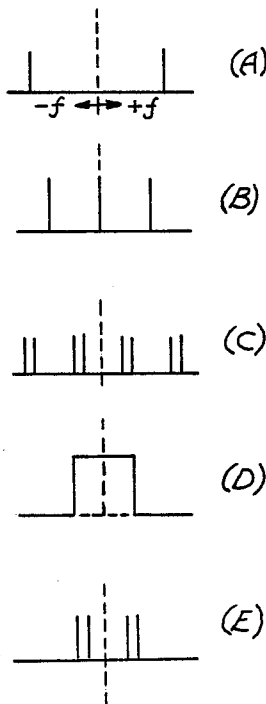


Fig. 10

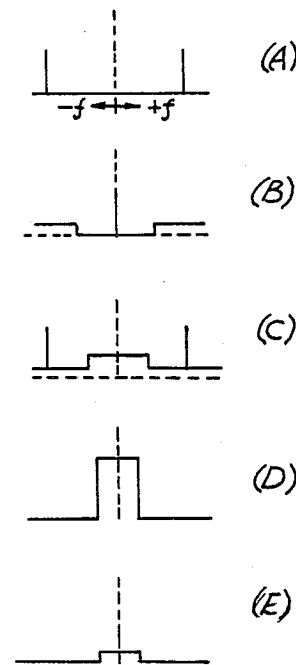


Fig. 11

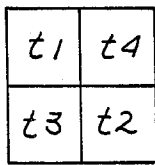


Fig. 12

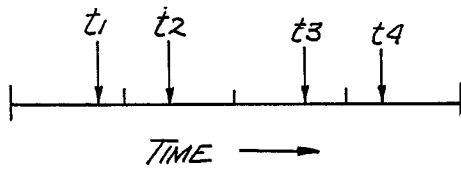


Fig. 13

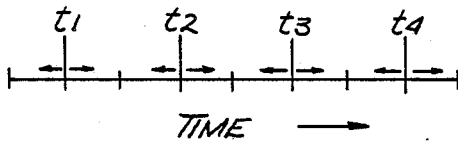


Fig. 14

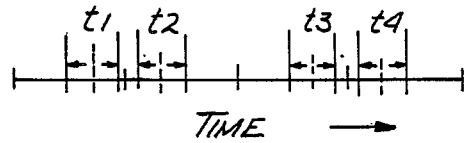


Fig. 15

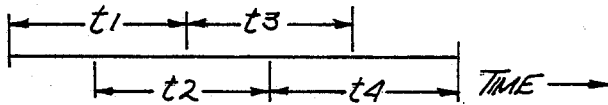


Fig. 16

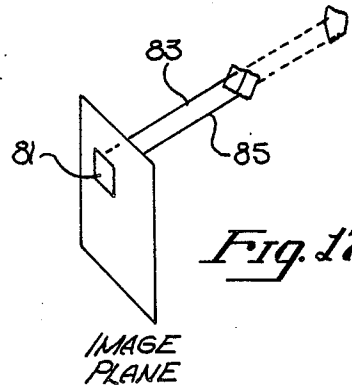


Fig. 17

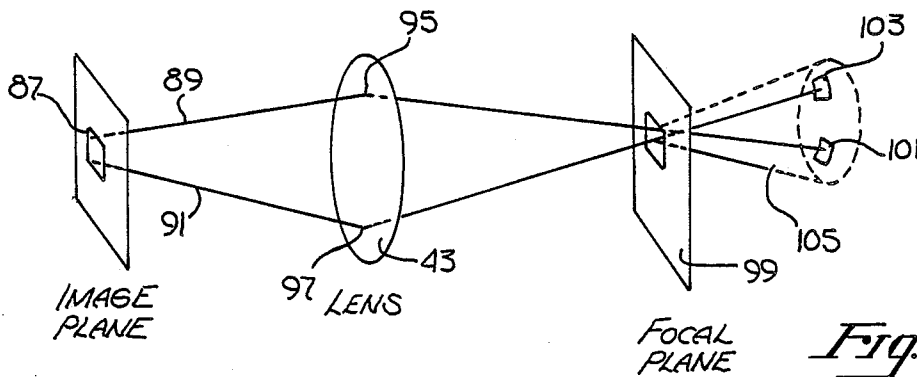


Fig. 18

Fig. 19

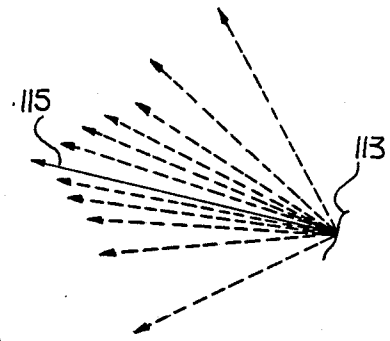
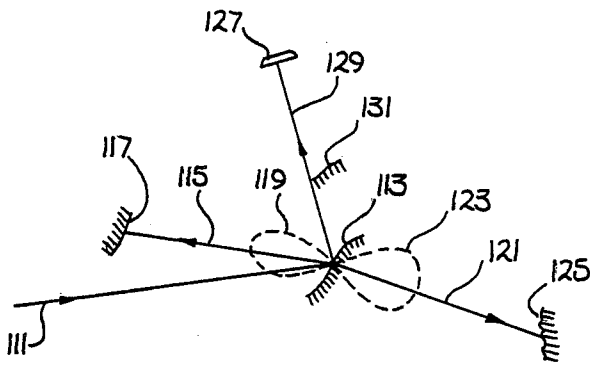


Fig. 20

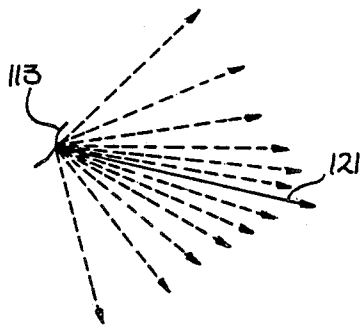


Fig. 21

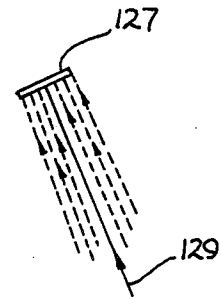


Fig. 22

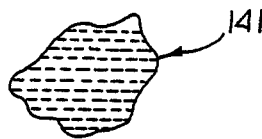


Fig. 23

PSEUDO-RANDOM POINT SAMPLING TECHNIQUES IN COMPUTER GRAPHICS

BACKGROUND OF THE INVENTION

This invention relates generally to the art of computer graphics, and more specifically to the field of point sampling of visual scene information for the purpose of reconstructing an image of the visual scene.

One form of computer graphics that is becoming widely practiced is to develop the sequence of video image frames of a moving object scene from information of the scene that has been stored in a computer memory. The object scene database contains information of the visual characteristics of the object scene, such as color, as well as information of movement. The creator of a sequence of video frames then uses a computer to electronically assemble signals of each video frame from the database in a manner that provides the views and movement of the object scene that is desired by the operator to be displayed.

The electronic signal for each video frame is typically developed by electronic sampling of the object scene database. A separate set of digital signals is developed to represent the color and/or intensity of each pixel of a standard raster scanned video monitor, for each video frame produced. Each pixel is thus the smallest resolution element of the video display. The color and/or intensity of each pixel is determined by sampling the database information to determine the characteristics of the object scene at the location of a given pixel. Such sampling is generally done by averaging the object scene information over a certain portion of the area of the pixel, or, more commonly, to sample the information at one or more points within the pixel, usually in some form of a periodically repeating pattern.

Recent developments in the field of computer graphics have been directed to increasing the realism of the resulting images. Progress has been made in more faithfully reproducing object textures, shadows, reflections and transparencies, for example. Much effort has been directed to the problem of aliasing, as well. Existing sampling techniques tend to generate video image frames having "alias" images; that is, images that appear to be real but which are not specified in the computer database. This is generally recognized as a characteristic of images formed through variously used point sampling techniques.

Therefore, it is a general object of the present invention to provide computer graphics techniques that further improve the realism of the resulting video image frames and the totality of video productions generated from computer database representations of an object scene.

SUMMARY OF THE INVENTION

This and additional objects are accomplished by the present invention wherein, briefly and generally, the object scene information in the computer database is sampled by points that are pseudo-randomly distributed in one or several functions or dimensions. According to one aspect of the invention, the point samples are pseudo-randomly distributed in a particular manner across the video image plane being constructed. According to another aspect, the pseudo-random distribution of point samples is taken over the time that is occupied by the video image frame being constructed. This substantially reduces or eliminates the undesirable aliasing, both spa-

tially and temporally. The distribution of samples over time also increases the realism of the video frame by adding the image blurring that would occur if the object scene was being photographed according to usual techniques.

According to another aspect of the present invention, a video frame is constructed to have a depth of field by sampling the data base as if the object scene represented by it is being viewed through a lens of a limited aperture that will view in focus only a limited depth of the object scene. The point samples are pseudo-randomly directed over a defined lens aperture when sampling the database information.

According to another specific aspect of the present invention, reflective and transparent characteristics of an object are taken into account by recognizing the degree of diffusion that occurs at each sample point. A particular angle of reflection or refraction is pseudo-randomly selected for each sample point from a range of possible angles depending upon the object characteristics. This adds realism to the resultant image by recognizing the diffuse, blurry nature of reflections and translucency that is possessed by most real objects.

According to yet another aspect of the present invention, an intensity distribution is specified for a light source that is illuminating the object scene. A single light source ray is pseudo-randomly selected from the specified light source distribution, for each sample point. This technique has the advantage of eliminating harsh shadows that result from existing techniques, further adding to the improved realism of the images, when a light source is only partially obscured.

Additional objects, advantages and features of the various aspects of the present invention will become apparent from the description of its preferred embodiments, which description should be taken in conjunction with the accompanying drawings.

BRIEF DESCRIPTION OF THE DRAWINGS

FIG. 1 illustrates generally a computer system that is suitable for carrying out the various aspects of the present invention;

FIG. 2 illustrates one possible form of object scene information that is stored in the computer memories of FIG. 1;

FIGS. 3 and 4 illustrate two existing point sampling techniques;

FIGS. 5, 6 and 7 show three specific embodiments of the pseudo-random spatial techniques of the present invention;

FIG. 8 illustrates spatial aliasing of the prior art techniques of FIGS. 3 and 4;

FIG. 9 illustrates the improvement brought about by the pseudo-random point sampling techniques of the present invention;

FIG. 10 shows a Fourier transform of a periodically sampled signal;

FIG. 11 shows a Fourier transform of a pseudo-randomly sampled signal;

FIG. 12 illustrates generally the distribution of the point samples over time;

FIGS. 13, 14, 15 and 16 illustrate several specific embodiments of the pseudo-random time sampling aspect of the present invention;

FIG. 17 illustrates generally computer database sampling by a given distribution of sample points on an image plane;

FIG. 18 shows a sampling technique that provides an image with a depth of field;

FIG. 19 is a ray tracing example for a single sample that includes the effects of reflection, refraction and light source distribution;

FIGS. 20, 21 and 22 illustrate additional details of the example shown in FIG. 19; and

FIG. 23 provides yet another application of the general techniques of the present invention.

DESCRIPTION OF THE PREFERRED EMBODIMENTS

Referring initially to FIG. 1, a general computer system as illustrated that is suitable for carrying out the various aspects of the present invention to be described in detail below. A common bus 11 is connected to a central processing unit (CPU) 13 and main memory 15. Also connected to the bus 11 is keyboard 17 and a large amount of disk memory 19. Either a commercially available VAX-11/780 or Cray large computer system is satisfactory. A frame buffer 21 receives output information from the bus 11 and applies it, through another bus 23, to a standard color television monitor 25 or another peripheral 27 that writes the resulting image frames directly onto film, or both. Additionally, an output device can simply be a videotape recorder of the standard type.

FIG. 2 illustrates the organization of the information of the object scene that is maintained in memory in the computer system of FIG. 1. There are many ways to store such information, one being selected for illustration in connection with the present invention. This technique involves breaking down the object scene into components, these elements being referred to herein as geometric primitives. One such geometric primitive is a polygon 31, for example, illustrated in FIG. 2 within an overlay 33 that shows in dotted outline a few adjacent pixels of the resulting display. The resulting display, of course, shows the color and intensity of the object scene within each pixel to be uniform, the size of the pixel being the resolution element size of display. The polygon represents portions of the object scene to be represented in a video frame.

The information stored in the computer memory for each object polygon is as extensive as necessary for producing a particular quality video image frame. Its position certainly must be a piece of that information, conveniently specified by the x, y and z coordinates. The x, y and z coordinates of each of the corner points of the polygon are stored for each video frame to be constructed, as shown in FIG. 2 with respect to the polygon 31. The "x" and "y" numbers represent, of course, the horizontal and vertical positions, respectively, of the points, while the "z" number specifies its distance behind the video frame (image plane) being constructed.

In order to be able to sample movement of the object scene that occurs in the time period of one image frame, a technique described in detail below, information is also maintained for each polygon of its movement during such time period. In FIG. 2, a second position 31' of the same polygon is illustrated with its corner point coordinates being stored as incremental changes over that of their initial positions. The position shown for the polygon 31 is preferably, for example, that at the beginning of a video frame, while the position 31' is that at the end of the video frame. The polygon can also change its shape during this time period.

Besides the positions of each object surface polygon being stored in the data base, certain visual characteristics are stored for each, as well. These include separate red, green and blue color reflection signals, red, green and blue transparency signals, extent of light diffusion upon reflection, extent of light dispersion upon transmission through the surface, and similar characteristics. The use of these and others are explained below in connection with the techniques of the present invention.

Referring to FIG. 3, a commonly used technique for determining the color and/or intensity of each pixel of the image frame is illustrated. The information in the computer database, in this example that of the polygons illustrated in FIG. 2, that is present in the space occupied by a particular pixel is determined for a plurality of points within the pixel. A large number of points are illustrated in FIG. 3, being periodically distributed in both dimensions, but there are even some techniques that use only one or a very few sample points per pixel. The nature of the object scene in each such sample point is determined, and those determinations are combined in some manner, such as by weighted or unweighted averaging, in order to determine the color and intensity of that pixel of the image frame.

FIG. 4 illustrates a similar periodic point sampling technique, except that not all point samples are taken in each case. Rather, the full density of the periodic sampling pattern is employed only in regions of a pixel where changes in the object scene occur, such as represented by a line 35. This image dependent technique thus reduces the number of samples and the processing time required.

But these and other periodic sampling techniques result in reconstructed images that include "aliases" of the real image to be displayed. Much effort has been directed to anti-aliasing techniques, one approach being to process the video signal obtained from a periodic pattern point sample technique in order to eliminate the aliasing effects of the technique. Others have suggested sampling in a non-periodic, dithered manner for a number of specific sampling applications. The techniques of the present invention include improvements to and new applications of such prior approaches.

Three different specific pseudo-random sampling techniques are illustrated in FIGS. 5, 6 and 7, wherein a single pixel is illustrated and, for simplicity of illustration, only four point samples per pixel are described. However, an actual implementation would likely use sixteen, or even as many as sixty-four samples per pixel, if all of the aspects of the present invention are utilized. For other specific implementations, a lesser number of samples, such as one per pixel, could be utilized. But in any event, the pattern of point samples, both within each pixel and across the face of the image frame in its entirety, are non-periodic, and form a non-rectangular and non-rectilinear grid pattern. Further, each selected sampling pattern may, alternatively, extend over an area of multiple pixels or only part of a pixel. But the examples described herein use a sampling area coincident to that of one pixel, for simplicity of explanation.

Each of the embodiments of FIGS. 5, 6 and 7 determines the location of the sample points within the pixel by first dividing the pixel into a number of non-overlapping areas equal to the number of sample points, in this case four. A sample point is confined within each such area, thus aiding in keeping the sample points spread out. The four areas of the pixel are labeled in the Fig-

ures as numbers 41, 43, 45 and 47. The areas are shown to be rectangular but can be some other shape.

In the embodiment of FIG. 5, the location of the sample point for each of these four areas is pseudo-randomly determined. Ideally, the "random" numbers to be used to determine their locations are purely random, but since they are so determined by computer, there is some element of repetitiveness of sample position within its defined area, although the distribution of locations of a large number of sample locations matches that of a random distribution. The most common way for a computer to generate the x,y coordinates of each sample point is to use a look-up table maintained in memory that has a list of numbers with a distribution being that of a random set of numbers. But the usual technique is for the computer to step through the table of numbers in sequence, so there are some repetitions since the table of numbers has finite length. However, the length of the list of numbers can be quite large so that repetition does not occur for a significant number of sample points. But in order to adequately describe both a completely random selection of sample locations and one controlled by such a computer look-up table, the locations are referred to here in this description as "pseudo-random".

In an implementation of the technique of FIG. 5, the same sample pattern is used on every pixel in a given image frame. It is preferable, however, to eliminate all periodicity of the sample pattern, including making sure that no two adjacent pixels have the same sample pattern. This can be done by using a sufficiently long look-up table of random numbers. It is preferable to generate a sample pattern with no two adjacent pixels (including those diagonally adjacent) having the same pattern, a result of the techniques shown in FIGS. 6 and 7.

Referring to FIG. 6, each of the four non-overlapping areas of the pixel illustrated has a reference point positioned at a fixed location in each, such as its middle. Each actual sample point location is then determined by the computer by adding a random positive or negative number to each of the reference point's x and y coordinates. These offset numbers are randomly determined, such as from the computer random number look-up table, and so repetition of the pattern would not occur for some very large number of pixels.

Another application of the same offset technique is a combination of the techniques of FIGS. 5 and 6, as shown in FIG. 7. This is similar to that of FIG. 5 and differs from that of FIG. 6 by having its reference points distributed rather than fixed in the middle of the adjacent pixel areas. The reference point pattern of the embodiment of FIG. 7 may be the same for each pixel, but the actual point sample locations are determined by adding a positive or negative x,y coordinate offset increment to the coordinates of each reference point. For convenience, a limit is placed on the maximum offset of each, as indicated by the dotted outline around each of the reference points of FIG. 7. The sample points in the embodiment of FIG. 6, however, can be located anywhere within its respective portion of the area of the pixel.

By first defining non-overlapping areas in which a single sample point lies, bunching up of sample points is avoided. It can be visualized that if each of the four sample points could be positioned anywhere within the entire pixel, there would be occasions, because of the random selection of those specific locations, where two or more of the sample points would be bunched to-

gether. Although defining a range of potential point sample locations to be within a non-overlapping area accomplishes this, there could obviously be some variations of this specific technique, such as by allowing the areas to overlap slightly, or some other variation. It may even cause no problem in particular applications if the sample points are chosen in a manner that their bunching together does occur occasionally.

Each of the specific techniques described with respect to FIGS. 5, 6 and 7 provides a picture sampled from a computer database that has fewer aliased images than if a periodic point sample distribution is utilized. The technique shown in FIG. 5, wherein the same pattern is repeated for each pixel of the image frame, provides some improvement, but the techniques according to FIGS. 6 and 7 are significantly better in reducing aliasing. The technique of FIG. 7 has been observed to be the best of the three because it has an additional advantage of being less noisy.

Referring to FIG. 8, an example of how an aliased image can be obtained and displayed is given. FIG. 8(A) is a "picket fence" image of "slats" 51, 53, 55, 57 and 59. This image is being sampled by a periodic distribution of points 61, 63, 65, 67 and 69, shown only in a single dimension for simplicity. Since the period of the sample points is greater than that of a periodic intensity variation of the image, all of those variations will not be faithfully reproduced. FIG. 8(B) shows the image of a video display that is developed from the samples of FIG. 8(A), region 71 being of one intensity and region 73 being of the other. Of course, the image of FIG. 8(B) is not a faithful reproduction of the image of FIG. 8(A). But since three of the sample points hit a portion of the image having one intensity and the other two a portion of the image having the other intensity, the detail of the other variations cannot be faithfully reproduced. The curve of FIG. 8(C) represents the intensity variation of the image of FIG. 8(A), the curve of FIG. 8(D) being the sampling function, and the curve of FIG. 8(E) illustrating the resulting image of FIG. 8(B).

One way that has been suggested to avoid forming such alias images is to increase the number of sample points so that the detail can be captured. That is to say, increase the number of samples in order to increase the well-known Nyquist limit. But to use extra sample points for this increases the computational complexity and can never really solve the problem; it only reduces its appearance somewhat. No matter how many samples are used, however, there will always be some situations of aliasing, particularly when the scene is changing. In this case, such a picket fence can show as a flashing black-and-white image over a large area, a very undesirable result.

Referring to FIG. 9, the effect of a randomly distributed pattern of sample points is illustrated. FIG. 9(A) assumes the same "picket fence" image in the computer database, as with FIG. 8(A). But the sample points in FIG. 9(A) are distributed non-periodically so that the resulting image of FIG. 9(B) appears to be gray rather than having large areas that are all white or all black. The image of FIG. 9(B) appears gray since alternate portions of the image are black-and-white, rather than having large areas of each color as in FIG. 8(B). Further, as the point samples of FIG. 9(A) are scanned relative to the "picket fence" image, there will be some noisy visual effect, similar to film grain noise, but one of considerably less annoyance than a large area flashing

black or white. The noise level is controlled by the number of samples per unit area.

FIGS. 10 and 11 show in the frequency domain the effect of periodic and stochastic point sampling, respectively. In both of FIGS. 10 and 11, curves (A) are the same, being an original signal, chosen to be a sine wave in the space domain. Curves (B) differ, however, in that FIG. 10(B) shows the frequency distribution of a spatially periodic sampling pattern, while FIG. 11(B) shows the frequency distribution of the ideal stochastic sampling pattern. In both cases, the sampling frequency is assumed to be below the Nyquist limit of the original signal, so will not be able to faithfully reproduce the original signal. But the comparison of the curves of FIGS. 10 and 11 show the anti-aliasing effect of a random distribution. The spatial sampling distribution across the image is preferably chosen so that a Fourier transform of such a distribution over an infinite plane approximates a Poisson disk distribution, as shown in FIG. 11(B). The primary characteristics of such a distribution include a very high level at zero frequency, a substantially zero magnitude to a certain frequency (both positive and negative), and then a substantially constant magnitude at higher frequencies. Except at zero frequency, the sampling function in the frequency domain (FIG. 11(B)) is substantially continuous. Such a distribution in the frequency domain provides the desired spatial position randomness and avoids bunching of the sample points. The techniques described with respect to FIGS. 5-7 approximate such a distribution.

The distribution (C) in each of FIGS. 10 and 11 shows the sampled signal in each of those examples, the result of convolving the signal of curve (A) with the sampling distribution of curve (B). In the periodic spatial sample example of FIG. 10, a number of extraneous spikes are obtained since each of the sampling spikes of FIG. 10(B) is individually convolved with each of the spikes of the signal of FIG. 10(A). Since the frequencies of the signal of FIG. 10(A) are in excess of that of the sampling function of FIG. 10(B), the sampled signal of FIG. 10(C) is not a faithful reproduction of that of the original signal. When the sampled signal of FIG. 10(C) is displayed, it is in effect multiplied by a lowpass filter similar to that of FIG. 10(D). The resultant sampled signal is shown in FIG. 10(E), which is the portion of the signal of FIG. 10(C) which is within the band pass of the filter function of FIG. 10(D). The signal indicated at FIG. 10(E) is capable of reconstructing alias images that bear little or no resemblance to that of the original signal which was sampled.

The sampled signal of FIG. 11(C) also does not correspond with the original signal of FIG. 11(E), but when multiplied by its filter characteristics of FIG. 11(D), the resultant sampled signal of FIG. 11(E) is uniform over the frequency range of the filter. This produces in an image white noise, which is much preferable to reconstructing an apparent genuine image that does not exist.

The techniques described with respect to FIGS. 5-7 can also be utilized in a sampling system that modifies the sampling pattern in response to the content of the image information being sampled, so called adaptive sampling. For example, if image changes or detail within a portion of a sampling area required it, the pattern of sample points can be repeated in such an area portion in reduced scale.

According to another aspect of the present invention, similar sampling techniques are employed over time in order to add realistic motion blur, such as exist in video

and film techniques. Referring initially to FIG. 12, the example pixel of FIGS. 5-7 is indicated to have each of its four samples taken at different times t_1 , t_2 , t_3 and t_4 , regardless of the specific technique used to spatially locate the point samples. These times are selected to be within an interval that corresponds to a typical shutter opening for video frame acquisition which these techniques are intended to simulate. Therefore, if there is movement of the objects during the interval of a single frame indicated in the computer database, then the resultant image of that frame reconstructed from the samples being taken of the database information will similarly show motion blur.

In order to reduce or substantially eliminate temporal aliasing, the distribution in time of the samples over the frame interval is pseudo-randomly determined. Referring to FIG. 13, a time line is given wherein four non-overlapping intervals of time are designated as boundaries for each of the four sample points to occur. A pseudo-random selection of the time for each sample within each of these intervals is what is shown in FIG. 13. The same time distribution in FIG. 13 could be used for each pixel of the image frame being constructed, but is preferable that the sample times be different for at least each of immediately adjacent pixels, in order to maximize the anti-aliasing that is desired. Temporal aliasing can occur when changes occur in the scene, such as a flashing light, more rapidly than samples are being taken. It will also be recognized that the distribution in time illustrated in FIG. 13 involves the same considerations as the spatial distribution described with respect to FIG. 5.

Similarly, FIGS. 14 and 15 illustrate pseudo-random temporal sampling that is carried out in the same way as the spatial sampling described with respect to FIGS. 6 and 7, respectively. In FIG. 14, the time of each sample is chosen to be a pseudo-randomly determined offset from the center of the interval designated for each sample to occur. In FIG. 15, a reference time is pseudo-randomly determined for each sample within its interval, and then the actual time for each sample is determined as a shift from this reference an amount that is pseudo-randomly determined within certain limits. In each case, the time distribution of the samples is such that its Fourier transform preferably approximates a Poisson disk distribution, in the same manner as discussed above with respect to FIG. 11(B) for the samples' spatial distribution.

The time intervals set aside for each of the samples need not always be non-overlapping. An example of overlapping intervals is given in FIG. 16, the exact sample time being selected according to either of the techniques of FIGS. 14 or 15. But the difference in the example of FIG. 16 is that the probability is increased of the samples being weighted in the middle of the time interval of the image frame. This stimulates a film shutter that opens and closes relatively slowly so that motion of the object scene during the middle interval of the shutter opening contributes more to the intensity of the resulting blurred image than does motion occurring near the shutter opening or closing. Regardless of which of the specific techniques for determining the time distribution of the samples of a particular pixel are used, the total time period in which all of the samples of all pixels of a given image frame are taken is the same specified time interval represented in FIGS. 13-16 by the length of the time lines.

Referring to FIG. 17, a method is illustrated for sampling the polygons of the object scene in the computer database by the spatial and temporal sampling techniques described above. A pixel 81 is shown, as an example, as one of a large number combined together to form an image on a video screen (image plane). Rays 83 and 85 are projected behind the image plane from each of two of the point samples within the pixel 81. The spatial location of these point samples has been determined by one of the techniques described above. Their individual rays are then projected, usually perpendicularly to the image plane, to determine the nearestmost polygons that are intersected by the rays at their selected time of sample. Much work has been done on such ray tracing techniques and involves a significant computer sort and matching of the x,y coordinates of the sample points with those of the polygons in the computer database at the instant designated for the taking of each sample. Usually, more than one polygon will exist at each x,y sample location, so the computer also determines from the "z" information of them which is the closest to the image plane, and that is then the one that provides the visual information (color, etc.) of the object scene at that point. All of the visual characteristics determined for each of the samples of a given pixel are then averaged in some manner to form a single visual characteristic for that pixel for display during that frame.

Most computer graphics techniques show the entire object scene for each frame in focus, as if it was being viewed through a pinhole camera. This, of course, is not an accurate simulation of the real world of cameras and lenses, which have a limited depth of field. Depth of field can be taken into account by a ray tracing technique illustrated in FIG. 18. A single pixel 87 has two sample points with rays 89 and 91 extending from them behind the image plane. The depth of field technique illustrated in FIG. 18 is independent of the spatial and temporal sampling techniques described above, but it is preferable that those techniques be used in combination with the depth of field techniques being described in order to maximize the realism of the resulting image frames.

The example rays 89 and 91 of FIG. 18 do not extend directly behind the image plane, as was described with respect to FIG. 17, but rather are directed to intersect a simulated lens 93 at points 95 and 97, respectively. These rays then are directed again toward each other, under influence of refraction of the simulated lens. The rays intersect a focal plane 99 of the simulated optical system in the same pattern as exists on the image plane, as a result of defining the simulated optical system. The sample point rays 89 and 91 will then intersect polygons 101 and 103, respectively. Only polygons within the cone 105, shown in dotted outline, will be intersected with rays from sample points of the pixel 87, as defined by the characteristics of the optical system. Those polygons that are close to the focal plane 99 will contribute to a focused reconstructed image, while those further removed from the focal plane 99 contribute to an unfocused reconstructed image. In a computer software implementation of this technique, it has been found preferable to shift the x,y coordinates of the polygons an amount dependent upon their z distance from the focal plane 99 and the characteristics of the simulated optical system, and then proceed with the sampling in a manner similar to that shown in FIG. 17.

But whatever specific implementation is carried out, the technique has the advantage of adding considerable realism to the simulated image at the time that the image is first formed by sampling the database. Intersection of sample rays with the simulated lens 99 occurs over its entire defined aperture. In order to further reduce aliasing, the location of points of intersection of the rays with the lens, such as the points 95 and 97 shown in FIG. 18, are pseudo-randomly determined in the same manner as the earlier described pseudo-random determination of the spatial location and time of each sample point.

Other unrealistic effects that result from the use of existing computer graphics techniques are sharp shadows, glossy reflections, and, if translucency of objects is taken into account at all, that also results in sharp images showing the translucent objects. This, of course, is not the real world of diffuse objects and extended light sources, but are required simplifying assumptions under previous algorithms in order to maintain within reason the complexity of the calculations. But the distributed techniques of the present invention can also be applied to these tasks, in a similar manner as described previously, to add these realistic considerations. Referring to FIG. 19, a single ray 111 is traced from a single sample on the image plane (not shown) and interacts with the object scene in a manner specified by the characteristics of the light sources and object surfaces that are specified in the database. The techniques described with respect to FIG. 19 are independent of the techniques described earlier, but, of course, maximum realism is obtained if all of these techniques are combined together. What is to be described with respect to FIG. 19 occurs with each sample point of a particular image frame.

The ray 111 is first determined to strike a surface 113 of the object scene, as specified by one of the polygons whose characteristics are stored in the computer database. If this part of the object scene surface is reflective, a reflective ray 115 is then traced until it intersects another object scene surface 117. The object surface portion 117 may be observed in the completed image frame as a reflection in the object scene portion 113. But stored in the computer database is a diffusive light spread of the surface 113, as indicated by dotted outline 119 and shown separately in FIG. 20. If the characteristics of the surface 113 are specularly reflection, such as occurs with a mirror, the spread of possible ray reflection angles will be limited to essentially one. But most objects have some degree of diffusion and will scatter light incident upon them. Therefore, each sample point ray is traced in a manner to select one of the possible reflection angles, thereby to result in a realistic blurry reflection from diffusely reflecting surfaces since subsequent rays will be reflected off the surface 113 at one of the other possible angles shown in FIG. 20. The possible ray reflection angles, as shown in FIGS. 19 and 20, are weighted in one direction, as is actually the case in diffusely reflecting surfaces. And, as before, the particular direction taken by any given ray 115 is pseudo-randomly selected from the possible reflection angles.

The same consideration works in determining an angle of transmission of a ray 121 through the surface portion 113 if that surface portion is at all translucent. Assuming that it is, possible angles of refraction are stored in the computer database for that particular polygon, the distribution of such angles being indicated at 123 in FIG. 19 and also shown in FIG. 21. The spread of possible refractive angles depends, of course, on how

diffuse the translucency is. Plain glass, for example, will have a very narrow range of refractive angles, if not a single angle. And once the ray 121 is pseudo-randomly selected for a given sample point from the possible refractive angles, another portion 125 of the object scene can then be determined which is intersected by the ray 121 and is partially visible through the object portion 113.

In order to avoid sharp shadows, the realistic characteristics of an object scene illuminating light source 127 is taken into account. As shown in FIGS. 19 and 22, the light source 127 has a finite extended dimension, and is not always a point as often assumed in present computer graphics techniques. A ray 129 is traced from the illuminated surface 113 back to the source 127 to see if there is any other portion of the object scene, such as the portion 131, that will cause a shadow to be cast on the surface 113. As shown in the example of FIG. 19, the ray 129 will detect no such shadow, but other possible ray directions, as shown in FIG. 22, will be in the path of the object portion 131 and thus indicate that the object 113 is not illuminated by the source 127. The particular direction of the ray 129 is pseudo-randomly selected from those possible directions specified for the source 127, as shown in dotted outline in FIG. 22. In the example of FIG. 19, some of the rays will intersect the object portion 131 and some will not, resulting in soft, realistic shadows in the resulting image frame.

It will be recognized that each of the secondary surfaces intersected by rays, such as the surfaces 117 and 125 of FIG. 19, may also have reflective and translucent properties. The process is continued until such reflected or transparent images are so small in intensity as not to make any difference in the resulting image being constructed.

Referring to FIG. 23, an example is given of the broad extent of the techniques described above that are a part of the present invention. The techniques can be used to determine a center of mass of an object, an example of something that is desirable to be determined in the course of computer aided design (CAD). An object 141 of FIG. 23 has its surfaces determined by a pseudo-random distribution of sample points, shown to extend through the object in dotted outline. The pseudo-random nature of this sampling assures that the mea-

surement will be made on the actual object 141 and not some alias image of it.

The various techniques of the present invention have also been described by the inventors in a published paper, "Distributed Ray Tracing", Computer Graphics, Vol. 18, No. 3, pages 137-145, July, 1984, which is incorporated herein by reference. This paper includes photographs of images generated with the use of the various aspects of the present invention. The result of motion blur, as described with respect to FIGS. 12-16, is shown in FIGS. 3, 6 and 8 of that paper. Computer generated images having a depth of field are shown in FIGS. 4 and 5 of that paper, having been made by the techniques described with respect to FIG. 18 herein. FIG. 7 of that paper illustrates the shadowing and reflection techniques of the present invention that were described with respect to FIGS. 19-22 above.

Appendices A and B attached hereto are source code listings, in the C language, of computer programs implementing the various aspects of the invention described herein. They are part of a hidden surface algorithm. Appendix A is a general program that carries out the spatial sampling techniques of FIGS. 6 and 7 herein, one of which is optionally selected, temporal sampling of FIGS. 14 and 15 herein, depth of field of FIG. 18 herein, and secondary rays of FIGS. 19-22 for shadowing and reflection in a special image case. The resultant images of FIGS. 3, 5 and 7 of the above-referenced published paper, were made on a Cray computer with the source code listing of Appendix A.

Appendix B is a program that implements all of the aspects of the present invention for spherical objects and resulted in the images of FIGS. 4, 6 and 8 of the above-referenced published paper.

These computer programs contain material in which a claim of copyright is made by Lucasfilm, Ltd., the assignee hereof. This assignee has no objection to the duplication of Appendices A and B by photocopying and the like but reserves all other copyright rights therein.

Although the various aspects of the present invention have been described with respect to various preferred embodiments thereof, it will be understood that the invention is entitled to protection within the full scope of the appended claims.

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APPENDIX A

svvis.c

```
#ifndef lint
static char sccsid[] = "0(#)svvis.c 1.40 (Lucasfilm) 5/20/85";
#endif

#include <svvis.h>
#include <ctype.h>
#include <stdio.h>
#include <constants.h>

static int VisNewGrid(), VisEndBucket(), VisNewFrame(), VisEndFrame(), VisParam(), VisCamera(), VisVisa(VisGrid);
static int CSGNewTree(), CSGResolve();

static struct vis_proc VisProc = { VisNewGrid, VisEndBucket, VisNewFrame, VisEndFrame, VisParam, CSGNewTree, V

struct hbox {struct xyz min, max};
struct visiblepoint {
    struct visiblepoint *next;
};
```

```

struct xyz          v[4] ;
float              minz, maxx ;
struct color       color ;
struct color       trans ;
struct visflags    flag ;
float              glassbackopacity ;
#if CSG
short             csgtree ;
short             csnode ;
#endif CSG
};

float drand() ;
static float Pi;
static int Mmax, Maxx, Miny, Maxy ;
static int Border=1 ;
static float Hither, Yon ;
static int XPerBucket, YPerBucket, PixelsPerBucket, FiltersPerBucket ;
static int SamplesPerBucket ;
static int MaxSamplesPerBucket ;
static int BucketsAcrossScreen ;
static struct pixelrgb *Pixel ;
static struct visiblepoint **Point, *VisFreelist=0 ;
static int NVis=0, NVisInUse=0, NVisMaxUsed=0 ;
static int VisMallocSize=(16*1024-64) ;
static int Hit, Miss, Lerp ;

static float Focallength = 0 ;
static float FStop = 0 ;
static float FocalDistance = 0 ;
float Dofx_a, Dofx_b, Dofy_a, Dofy_b ;
int PinholeCamera=1 ;

static float FilterWidth = 2.0 ;
static int FilterType = 1 ;
static int BoxFilterFlag = 0 ;
static float boxfilter(x,y) float x,y ;
{ return (x>FilterWidth || y>FilterWidth) ? 0 : 1 ; }
static float gaussianfilter(x,y) float x,y ;
{ float w,d ;
  d=x*x+y*y;
  w=FilterWidth*FilterWidth/4.;
  return (d>w) ? 0 : exp(-d) - exp(-w);
}
static float sinc(r) float r ;
{ return (r<.001&& r>-.001) ? cos(2*r)/1 : sin(2*r)/r ; }
static float sincfilter(x,y) float x,y ;
{ return sinc(x)*sinc(y) ; }
static float bessel(r) float r ;
{ return (r<.001&&r>-.001) ? 1 : j1(2*r)/r ; }
static float besselfilter(x,y) float x,y ;
{ float r ;
  r = sqrt(x*x+y*y);
  return bessel(r);
}
static float bartlettfilter(x,y) float x,y ;
{ float ax,ay,w;
  ax = (x<0) ? -x : x;
  ay = (y<0) ? -y : y;
  w = FilterWidth;
  return (w<ax || w<ay) ? 0 : (w-ax)*(w-ay);
}
#define FILTERNAME 80
#define NFILTERS 5
static char FilterName[NFILTERS][FILTERNAME] =
{"box", "Gaussian", "sinc", "Bartlett",
"Bessel"} ;
static float (*FilterRoutine[NFILTERS])() =
{boxfilter, gaussianfilter, sincfilter, bartlettfilter,
besselfilter};

```

*drand**VisMallocSize**...box filter**box filter**gaussian filter**sinc**sinc filter**bessel**bessel filter**bartlett filter**float*

...float

```

#define NJITTER 512
static int JitterFlag=1;
static float XJitter[NJITTER], YJitter[NJITTER], TJitter[NJITTER];
static float LXJitter[NJITTER], LYJitter[NJITTER];
static struct xy *Location;
static float *Filter;
static struct xy *Lens;
static float MinXJitter=0, MaxXJitter;
static float MinYJitter=0, MaxYJitter;
static int NS;
static int NxGrid=4, NyGrid=4;

static struct xy Leas16[16] = {
    0.312500, 0.000000,
    -0.312500, 0.000000,
    0.750000, 0.000000,
    -0.750000, 0.000000,
    0.000000, 0.312500,
    0.000000, -0.312500,
    0.000000, 0.750000,
    0.000000, -0.750000,
    0.625000, 0.375000,
    0.375000, 0.625000,
    -0.625000, 0.375000,
    -0.375000, 0.625000,
    0.625000, -0.375000,
    0.375000, -0.625000,
    -0.625000, -0.375000,
    -0.375000, -0.625000 };

```

```

struct vis_procs *VisLoad() {
    Pi = 4*atan(1.0);
    return(&VisProcs);
}

```

VisLoad

```

static int VisCamera(focallength,fstop,focaldistance)
    float focallength, fstop, focaldistance;
{
    PinHoleCamera = (focallength==0.0);
    If (PinHoleCamera) return;

    If (focallength<0.0 || fstop<=0.0 || focaldistance<=0.0) {
        fprintf(stderr, "invalid arguments to visible surface camera routine:\n");
        fprintf(stderr, "\tfocal length   %f\n", focallength);
        fprintf(stderr, "\tf stop       %f\n", fstop);
        fprintf(stderr, "\tfocal distance %f\n", focaldistance);
    }
    FocalLength = focallength;
    FStop = fstop;
    FocalDistance = focaldistance;
}

```

VisCamera

```

static int VisCameraSetup()
{
    float lensradius;
    static struct xyz Aeye={0,0,1}, Beye={1,1,1};
    struct xy Ascreen, Bscreen;

```

VisCameraSetup

```

/* The perspective transformation from eye space to screen space assumes
 * a pinhole camera located at the origin in eye space, and transforms
 * each point (Xe,Ye,Ze) in eye space to a point (Xs,Ys,Zs) in screen
 * space. For depth of field, however, different sample points assume
 * pinhole cameras located at different points on the lens. A point
 * that is at (Xe,Ye,Ze) in eye space of the center of the lens is at
 * (Xcl,Ycl,Zc) in the eye space of the point (lensz,lensy,0) on the
 * lens, where
 * Xcl-Xe = lensz * ( 1 - Ze/focaldistance )
 * Ycl-Ye = lensy * ( 1 - Ze/focaldistance )
 * The values of lensz and lensy that we use are express as a fraction
 * of the effective lens radius, so that our formulas are actually
 * Xcl-Xe = lensz * lensradius * (1 - Ze/focaldistance)
 * Ycl-Ye = lensy * lensradius * (1 - Ze/focaldistance)
 * where

```

```

* lensradius = 0.5 * focallength / fstop
* We know that the perspective matrix is of the form
* a 0 0 0
* 0 b 0 0
* c d e f
* g h i 0
* so that
* Xs = (a*Xe + c*Ze + g) / (f*Ze)
* Ys = (b*Xe + d*Ze + h) / (f*Ze)
* and
* Xsl = (a*Xel + c*Ze + g) / (f*Ze)
* Ysl = (b*Xel + d*Ze + h) / (f*Ze)
* giving us
* Xsl-Xs = (Xel-Xe) * a/(f*Ze)
*         = lensx * lensradius * (a/f) * (1/Ze - 1/focaldistance)
*         = lensx * (Dofx_a/Ze + Dofx_b)
* Ysl-Ys = (Yel-Ye) * b/(f*Ze)
*         = lensy * lensradius * (b/f) * (1/Ze - 1/focaldistance)
*         = lensy * (Dofy_a/Ze + Dofy_b)
* These formulas are the ones we use to transform screen space points
* to account for different lens locations.
* We can calculate the key variables in these equations by finding the
* the screen space coordinates of the points A=(0,0,1) and B=(1,1,1):
* XsA = (a*0 + c*1 + g) / (f*1)
*     = (c+g)/f
*     XsB = (a+c+g)/f
*     XsB-XsA = a/f
*     YsB-YsA = d/f
* and it follows that
* Dofx_a = (XsB-XsA) * lensradius
* Dofy_a = (YsB-YsA) * lensradius
* Dofx_b = -Dofx_a/focaldistance
* Dofy_b = -Dofy_a/focaldistance
*/
  If (PinHoleCamera) return ;

  lensradius = 0.5 * FocalLength / FStop ;
  EyeToScreenXY(&Aeye,&Ascreen) ;
  EyeToScreenXY(&Beye,&Bscreen) ;
  Dofx_a = lensradius * (Bscreen.x - Ascreen.x) ;
  Dofy_a = lensradius * (Bscreen.y - Ascreen.y) ;
  Dofx_b = -Dofx_a / FocalDistance ;
  Dofy_b = -Dofy_a / FocalDistance ;
}

```

```

static int VisEndBucket(xb,yb)
  int xb,yb ;
{
  float *jx, *jy, *jt, *jlx, *jly ;
  int xy ;
  register int s, i ;
  register struct mpoly *mp ;
  struct mpoly *MpGetBucket() ;
  int left, right, top, bottom ;
  float alpha, salpha;
#if ALPHABETA
  float beta0, beta1, beta2, beta3, oma ;
#endif
  struct bbox bound(), box, speedbox ;
  struct bbox boundspeed() ;
  int xmin, xmax, ymin, ymax ;
  static struct xyz vertex[4], v[4] ;
  int nsample, pixel ;
  float locx, locy, dx, dy, lx, ly, rx, ry ;
  float ax, ay, bx, by, lensx, lensy ;

  left = Minx + xb*XPerBucket ;
  top = Miny + yb*YPerBucket ;
  right = left + XPerBucket - 1 ;
  bottom = top + YPerBucket - 1 ;
}

```

VisEndBucket

```

mp=MpGetBucket(xb,yb);
If (!mp) goto emptybucket;

bzero ((char *)Pixel, FiltersPerBucket*sizeof(struct pixelrgba) );
CalcSamplesPerBucket(mp) ;
bzero ((char *)Point, SamplesPerBucket*sizeof(struct visiblepoint *));
jx = &XJitter[(int)(23*drand())];
jy = &YJitter[(int)(23*drand())];
jt = &TJitter[(int)(23*drand())];
jlx = &LXJitter[(int)(23*drand())];
jly = &LYJitter[(int)(23*drand())];
for (; mp; mp=mp->next) {
    bcopy ((char *)mp->v,(char *)vertex,sizeof(vertex));
    vertex[0].x -= left;
    vertex[1].x -= left;
    vertex[2].x -= left;
    vertex[3].x -= left;
    vertex[0].y -= top;
    vertex[1].y -= top;
    vertex[2].y -= top;
    vertex[3].y -= top;
    box = bound(vertex);
    mp->min.z = box.min.z;
    mp->max.z = box.max.z;
    #if MOTIONBLUR && !GLOSS
        If (mp->flag.moving) {
            speedbox = bound(mp->speed);
            If (speedbox.min.z<0) box.min.z += speedbox.min.z;
            If (speedbox.max.z>0) box.max.z += speedbox.max.z;
            mp->min.z = box.min.z;
            mp->max.z = box.max.z;
        }
    #if DEPTHIOFFIELD
        If (!PinholeCamera)
            boundof (&box);
    #endif DEPTHIOFFIELD
    speedbox.min.x /= NS;
    speedbox.max.x /= NS;
    speedbox.min.y /= NS;
    speedbox.max.y /= NS;
    If (speedbox.min.x<0) box.min.x += speedbox.min.x;
    If (speedbox.max.x>0) box.max.x += speedbox.max.x;
    If (speedbox.min.y<0) box.min.y += speedbox.min.y;
    If (speedbox.max.y>0) box.max.y += speedbox.max.y;
    for (s=0; s<NS; s++) {
        salpha = s/(float)NS;
        locx = Location[s].x;
        locy = Location[s].y;
        lensx = Lens[s].x - .5/NS;
        lensy = Lens[s].y - .5/NS;
        xmin = box.min.x - locx - MaxXJitter;
        ymin = box.min.y - locy - MaxYJitter;
        xmax = box.max.x - locx /* + MinXJitter */;
        ymax = box.max.y - locy /* + MinYJitter */;
        If (xmin<0) xmin=0;
        If (xmax>=XPerBucket) xmax=XPerBucket-1;
        If (ymin<0) ymin=0;
        If (ymax>=YPerBucket) ymax=YPerBucket-1;
        for (y=ymin, dy=locy+ymin; y<=ymax; dy++, y++) {
            pixel = y*XPerBucket + xmin;
            ssample = pixel*NS+s;
            i = 7*s + 2*pixel;
            for (x=xmin, dx=locx+xmin; x<=xmax; ssample+=NS, i+=2, dx++, x++) {
                alpha = salpha + jt[i+2];
            }
        }
    #if ALPHABETA
        oma = 1 - alpha;
        beta0 = alpha / (alpha + oma*mp->abratio[0]);
        beta1 = alpha / (alpha + oma*mp->abratio[1]);
        beta2 = alpha / (alpha + oma*mp->abratio[2]);
        beta3 = alpha / (alpha + oma*mp->abratio[3]);
    #else
    #define beta0 alpha
    #define beta1 alpha
    #define beta2 alpha
    #endif
}

```

```

#define beta3 alpha
#endif

v[0].x = vertex[0].x + beta0*mp->speed[0].x ;
v[1].x = vertex[1].x + beta1*mp->speed[1].x ;
v[2].x = vertex[2].x + beta2*mp->speed[2].x ;
v[3].x = vertex[3].x + beta3*mp->speed[3].x ;
v[0].y = vertex[0].y + beta0*mp->speed[0].y ;
v[1].y = vertex[1].y + beta1*mp->speed[1].y ;
v[2].y = vertex[2].y + beta2*mp->speed[2].y ;
v[3].y = vertex[3].y + beta3*mp->speed[3].y ;
v[0].z = vertex[0].z + beta0*mp->speed[0].z ;
v[1].z = vertex[1].z + beta1*mp->speed[1].z ;
v[2].z = vertex[2].z + beta2*mp->speed[2].z ;
v[3].z = vertex[3].z + beta3*mp->speed[3].z ;

#if DEPTHIOFFIELD
    if (!PinHoleCamera) {
        lx = lensx + jlx[i+3] ;
        ly = lensy + jly[i+4] ;
        ax = lx * Dofx_a ;
        ay = ly * Dofy_a ;
        bx = lx * Dofx_b ;
        by = ly * Dofy_b ;
        v[0].x += ax / v[0].z ;
        v[1].x += ax / v[1].z ;
        v[2].x += ax / v[2].z ;
        v[3].x += ax / v[3].z ;
        v[0].y += ay / v[0].z ;
        v[1].y += ay / v[1].z ;
        v[2].y += ay / v[2].z ;
        v[3].y += ay / v[3].z ;
        rx = dx + jx[i] - bx ;
        ry = dy + jy[i+1] - by ;
    }
    else
    {
        rx = dx + jx[i] ;
        ry = dy + jy[i+1] ;
    }
    v[0].x -= rx ; v[0].y -= ry ;
    v[1].x -= rx ; v[1].y -= ry ;
    v[2].x -= rx ; v[2].y -= ry ;
    v[3].x -= rx ; v[3].y -= ry ;
    sample(asmample,mp,v) ;
}
box.min.x += speedbox.min.x ;
box.max.x += speedbox.max.x ;
box.min.y += speedbox.min.y ;
box.max.y += speedbox.max.y ;
}
else
#endif
{
#if DEPTHIOFFIELD
    if (!PinHoleCamera) {
        bounddof (&box) ;
    }
    #if GLOSS
        float d ;
        d = sqrt (mp->speed[0].x*mp->speed[0].x +
            mp->speed[0].y*mp->speed[0].y +
            mp->speed[0].z*mp->speed[0].z) ;
    #endif
    #endif
    v[0].z = vertex[0].z ;
    v[1].z = vertex[1].z ;
    v[2].z = vertex[2].z ;
    v[3].z = vertex[3].z ;
    for (s=0; s<NS; s++) {
        locx = Location[s].x ;
        locy = Location[s].y ;
        lensx = Lens[s].x - .5/NS ;
        lensy = Lens[s].y - .5/NS ;

```



```

xmin = box.min.x - locx - MaxXJitter ;
ymin = box.min.y - locy - MaxYJitter ;
xmax = box.max.x - locx /* + MinXJitter */ ;
ymax = box.max.y - locy /* + MinYJitter */ ;
if (xmin<0) xmin=0 ;
if (xmax>=XPerBucket) xmax=XPerBucket-1 ;
if (ymin<0) ymin=0 ;
if (ymax>=YPerBucket) ymax=YPerBucket-1 ;
for (y=ymin, dy=locy+ymin; y<=ymax; dy++, y++) {
    pixel = y*XPerBucket + xmin ;
    nsample = pixel*NS+s ;
    i = 7*s + 2*pixel ;
    for (x=xmin, dx=locx+xmin; x<=xmax; nsample+=NS, i+=2, dx++, x++) {
        lx = lessx + jlx[i+3] ;
        ly = lessy + jly[i+4] ;

        lx *= d ;
        ly *= d ;

        ax = lx * Dofx_a ;
        ay = ly * Dofy_a ;
        bx = lx * Dofx_b ;
        by = ly * Dofy_b ;
        rx = dx + jx[i] - bx ;
        ry = dy + jy[i+1] - by ;
        v[0].x = vertex[0].x - rx + ax/vertex[0].z ;
        v[1].x = vertex[1].x - rx + ax/vertex[1].z ;
        v[2].x = vertex[2].x - rx + ax/vertex[2].z ;
        v[3].x = vertex[3].x - rx + ax/vertex[3].z ;
        v[0].y = vertex[0].y - ry + ay/vertex[0].z ;
        v[1].y = vertex[1].y - ry + ay/vertex[1].z ;
        v[2].y = vertex[2].y - ry + ay/vertex[2].z ;
        v[3].y = vertex[3].y - ry + ay/vertex[3].z ;
        sample(nsample,mp,v) ;
    }
}
} else
endif
(
    v[0].z = vertex[0].z ;
    v[1].z = vertex[1].z ;
    v[2].z = vertex[2].z ;
    v[3].z = vertex[3].z ;
    for (s=0; s<NS; s++) {
        locx = Location[s].x ;
        locy = Location[s].y ;
        xmin = box.min.x - locx - MaxXJitter ;
        ymin = box.min.y - locy - MaxYJitter ;
        xmax = box.max.x - locx /* + MinXJitter */ ;
        ymax = box.max.y - locy /* + MinYJitter */ ;
        if (xmin<0) xmin=0 ;
        if (xmax>=XPerBucket) xmax=XPerBucket-1 ;
        if (ymin<0) ymin=0 ;
        if (ymax>=YPerBucket) ymax=YPerBucket-1 ;
        for (y=ymin, dy=locy+ymin; y<=ymax; dy++, y++) {
            pixel = y*XPerBucket + xmin ;
            nsample = pixel*NS+s ;
            i = 7*s + 2*pixel ;
            for (x=xmin, dx=locx+xmin; x<=xmax; nsample+=NS, i+=2, dx++, x++) {
                rx = dx + jx[i] ;
                ry = dy + jy[i+1] ;
                v[0].x = vertex[0].x - rx ;
                v[1].x = vertex[1].x - rx ;
                v[2].x = vertex[2].x - rx ;
                v[3].x = vertex[3].x - rx ;
                v[0].y = vertex[0].y - ry ;
                v[1].y = vertex[1].y - ry ;
                v[2].y = vertex[2].y - ry ;
                v[3].y = vertex[3].y - ry ;

```

```

        sample(asample,mp,v) ;
    }
}
}
}

CSGResolve() ;
filter() ;
freepoints() ;

DisplayWindow (Pixel, left-Border, right+Border, top-Border, bottom+Border) ;

MpEmptyBucket(xb,yb) ;
return 1 ;

emptybucket:
DisplayWindow ((struct pixelsgba *)0, left-Border, right+Border, top-Border, bottom+Border) ;
MpEmptyBucket(xb,yb) ;
return 0 ;
}

```

```
static int VisEndFrame()
```

VisEndFrame

```
{
    MpBucketEndFrame() ;
    DisplayEndFrame() ;
}
```

```
static int VisFilter(type,width)
```

VisFilter

```
char *type;
float width ;
{
    int i ;
    if (FilterWidth<=0.) goto Error;
    for(i=0;i<NFILTERS;i++) {
        if (!strcmp(type,FilterName[i])) {
            FilterType = i ;
            FilterWidth = width;
            BoxFilterFlag = (width==1.0 && !strcmp(type,"box"));
            return;
        }
    }
    fprintf (stderr, "The stochastic hider only has the following filters:\n");
    for(i=0;i<NFILTERS;i++)
        printf (stderr, "%s ",FilterName[i]) ;
    printf (stderr, "\n") ;
    return;
Error:
    printf (stderr, "Filter width must be >0\n") ;
}
```

```
static int VisNewFrame (minx,maxx,miny,maxy,xper,yper,sideways,hither,yon)
```

VisNewFrame

```
float hither, yon ;
{
    int ax ;

    Hither = hither ;
    Yon = yon ;
    Border = FilterWidth/2. + 0.499 ;
    XPerBucket = xper ;
    YPerBucket = yper ;
    PixelsPerBucket = XPerBucket * YPerBucket ;
    FiltersPerBucket = (XPerBucket+2*Border) * (YPerBucket+2*Border) ;
    tablesinit(NxGrid,NyGrid);
    MaxSamplesPerBucket = PixelsPerBucket * NS ;
    Minx = minx - Border ;
    Miny = miny - Border ;
    Maxx = maxx + Border ;
    Maxy = maxy + Border ;
}
```

...VisNewGrid

```

nx = Maxx - Minx + 1 ;
BucketsAcrossScreen = (nx+XPerBucket-1) / XPerBucket ;
If (Point) {
    free((char *)Point) ;
    free((char *)Pixel) ;
}
Point = (struct visiblepoint **) malloc ((unsigned)(MaxSamplesPerBucket * sizeof(struct visiblepoint *) )) ;
Pixel = (struct pixelrgba *) malloc ((unsigned)(FiltersPerBucket * sizeof(struct pixelrgba )) ) ;

VisCameraSetup() ;
MpbucketNewFrame (Minx, Maxx, Miny, Maxy, XPerBucket, YPerBucket, sideways, hither, you) ;
DisplayNewFrame (minx, maxx, miny, maxy, Border, XPerBucket, YPerBucket, sideways) ;

Hit = 0 ;
Lerp = 0 ;
Miss = 0 ;

return Border ;
}

```

```

static int VisNewGrid(g)
    struct grid *g;
{
    MpbucketNewGrid(g) ;
}

```

VisNewGrid

```

static int VisParam(ac,av) char **av; {
    int x,y;
    while(ac>0) {
        If (strcmp(*av,"grid")) {
            If (ac==1 || !isdigit(*av[1])) {
                NxGrid=4;
                NyGrid=4;
                av++;
                ac--;
            }
            else If (ac>=3) {
                x=atoi(av[1]);
                y=atoi(av[2]);
                If (x<-0 || y<=0) goto Error;
                NxGrid = x;
                NyGrid = y;
                av+=3;
                ac-=3;
            }
            else goto Error;
        }
        else If (strcmp(*av,"jitter")) {
            If (ac>=1) {
                JitterFlag = OnOff(av[1]);
                av+=2;
                ac-=2;
            }
            else
                JitterFlag = 1 ;
                av++;
                ac--;
        }
        else goto Error;
    }
    return ;
}
Error:
    fprintf (stderr,"The stochastic hider can take these parameters:\n");
    fprintf (stderr,"\tgrid %d %d\n");
    fprintf (stderr,"\tjitter on/off\n");
}

```

VisParam

```

static int VisPrint(s)
    char *s ;
{

```

VisPrint

```

if (s && (!strcmp(s,"stat"))) {
    register struct visiblepoint *vp ;
    register int n ;
    MpPrintStat() ;
    for (n=0, vp=VisFreeList; vp; vp=vp->next, n++) ;
    printf ("      Visiblepoints: %4d allocated", NVis) ;
    printf (" %4d kb", sizeof(struct visiblepoint)*NVis/1024) ;
    printf (" %4d used", NVisMaxUsed) ;
    printf (" %4d in use", NVisInUse) ;
    printf (" %4d free\n", n) ;
    n = Hit+Miss ;
    if (n==0) n=1 ;
    printf ("      Hider samples: %5.2f%% (%d hits and %d misses)\n",
        100.*Hit/(float)n, Hit, Miss) ;
    if (Hit)
        printf ("      Hider z lerps: %5.2f%% (%d lerps out of %d hits)\n",
            100.*Lerp/(float)Hit, Lerp, Hit) ;
}
else {
    printf ("      Hider:      stochastic sampler");
    printf (" (%d by %d samples per pixel)", NxGrid, NyGrid) ;
    printf (" jitter %s\n", JitterFlag?"on":"off" ) ;
    printf ("      Filter:      %s, %f pixels wide\n", FilterName[FilterType], FilterWidth) ;
    if (PinHoleCamera)
        printf ("      Camera:      pinhole\n") ;
    else {
        printf ("      Camera:      focal length %f\n",FocalLength) ;
        printf ("                  f stop %f\n",FStop) ;
        printf ("                  focal distance %f\n",FocalDistance) ;
    }
}
}

```

```
static struct bbox bound(v)
```

bound

```

    struct xyz v[4] ;
{
    struct bbox b ;

    if (v[0].x < v[1].x) {
        if (v[2].x < v[3].x) {
            b.min.x = (v[0].x < v[2].x) ? v[0].x : v[2].x ;
            b.max.x = (v[1].x > v[3].x) ? v[1].x : v[3].x ;
        }
        else {
            b.min.x = (v[0].x < v[3].x) ? v[0].x : v[3].x ;
            b.max.x = (v[1].x > v[2].x) ? v[1].x : v[2].x ;
        }
    }
    else {
        if (v[2].x < v[3].x) {
            b.min.x = (v[1].x < v[2].x) ? v[1].x : v[2].x ;
            b.max.x = (v[0].x > v[3].x) ? v[0].x : v[3].x ;
        }
        else {
            b.min.x = (v[1].x < v[3].x) ? v[1].x : v[3].x ;
            b.max.x = (v[0].x > v[2].x) ? v[0].x : v[2].x ;
        }
    }
    if (v[0].y < v[1].y) {
        if (v[2].y < v[3].y) {
            b.min.y = (v[0].y < v[2].y) ? v[0].y : v[2].y ;
            b.max.y = (v[1].y > v[3].y) ? v[1].y : v[3].y ;
        }
        else {
            b.min.y = (v[0].y < v[3].y) ? v[0].y : v[3].y ;
            b.max.y = (v[1].y > v[2].y) ? v[1].y : v[2].y ;
        }
    }
    else {
        if (v[2].y < v[3].y) {
            b.min.y = (v[1].y < v[2].y) ? v[1].y : v[2].y ;
            b.max.y = (v[0].y > v[3].y) ? v[0].y : v[3].y ;
        }
    }
}

```

...bound

```

    }
    else {
        b.min.y = (v[1].y < v[3].y) ? v[1].y : v[3].y ;
        b.max.y = (v[0].y > v[2].y) ? v[0].y : v[2].y ;
    }
}
if (v[0].z < v[1].z) {
    if (v[2].z < v[3].z) {
        b.min.z = (v[0].z < v[2].z) ? v[0].z : v[2].z ;
        b.max.z = (v[1].z > v[3].z) ? v[1].z : v[3].z ;
    }
    else {
        b.min.z = (v[0].z < v[3].z) ? v[0].z : v[3].z ;
        b.max.z = (v[1].z > v[2].z) ? v[1].z : v[2].z ;
    }
}
else {
    if (v[2].z < v[3].z) {
        b.min.z = (v[1].z < v[2].z) ? v[1].z : v[2].z ;
        b.max.z = (v[0].z > v[3].z) ? v[0].z : v[3].z ;
    }
    else {
        b.min.z = (v[1].z < v[3].z) ? v[1].z : v[3].z ;
        b.max.z = (v[0].z > v[2].z) ? v[0].z : v[2].z ;
    }
}
}
return b ;
}

```

#if DEPTHOFFIELD

bounddof(b)

struct bbox *b ;

```

{
    float b1, b2, zmin, zmax ;

```

/*if (PinHoleCamera) return ;*/

zmin = b->min.z ;

zmax = b->max.z ;

if (zmin < 111ther) zmin = 111ther ;

if (zmax > 100) zmax = 100 ;

b1 = Dofx_a/zmin + Dofx_b ;

b2 = Dofx_a/zmax + Dofx_b ;

if (b1 < 0) b1 = -b1 ;

if (b2 < 0) b2 = -b2 ;

if (b2 > b1) b1 = b2 ;

b->min.x -= b1 ;

b->max.x += b1 ;

b1 = Dofy_a/zmin + Dofy_b ;

b2 = Dofy_a/zmax + Dofy_b ;

if (b1 < 0) b1 = -b1 ;

if (b2 < 0) b2 = -b2 ;

if (b2 > b1) b1 = b2 ;

b->min.y -= b1 ;

b->max.y += b1 ;

#endif DEPTHOFFIELD

static CalcSamplesPerBucket(mp) register struct mpoly *mp ; { }

CalcSamplesPerBucket

static applyboxfilter()

applybox filter

```

{
    int x, y ;
    register int s ;
    register struct pixelrgb *p ;
    register struct visiblepoint **vpp, *vp ;
    register float onecovers ;
    int bb ;

```

filler

```

bb = 2*Border ;
onecovers = 1./((float)NS) ;
vpp = Point ;
vp = *vpp++ ;
p = Pixel + Border*(XPerBucket+bb) + Border ;
for (y=0; ++y<=YPerBucket; p+=bb) {
    for (x=0; ++x<=XPerBucket; p++) {
        for (s=0; ++s<=NS; vp=(*vpp++)) {
            if (vp && !vp->flag.matte) {
                p->r += onecovers * vp->color.r ;
                p->g += onecovers * vp->color.g ;
                p->b += onecovers * vp->color.b ;
                p->a += (vp->flag.opaque) ? onecovers : onecovers * (1.-
                    (vp->trans.r+vp->trans.g+vp->trans.b)*(1./3.)) ;
            }
        }
    }
}
}
}
}
static filter()
{
    int x, y ;
    register int j, i ;
    register float *f ;
    register struct pixelrgba *p ;
    register struct visiblepoint *vp ;
    register int s ;
    struct visiblepoint **vpp ;
    float alpha ;
    struct pixelrgba *ploop, *pp ;
    int fskip, pskip, pback ;
    int width, bb ;

    if (BoxFilterFlag) {
        applyboxfilter();
        return;
    }
    /* Set up increments so that in the inner loop:
     * f = 8(Filter/s*FilterWidth*FilterWidth+j*FilterWidth+i) ;
     * p = Pixel + (y+j)*(XPerBucket+2*Border) + x + i ;
     */
    bb = Border+Border ;
    width = 1 + bb ;
    fskip = width*width ;
    pskip = sizeof(*p) * (XPerBucket+bb-width) ;
    pback = sizeof(*p) * (width*(XPerBucket+bb)) ;
    for (y=0, p=Pixel, vpp=Point, vp=(*vpp++); ++y<=YPerBucket; p+=bb) {
        for (x=0; ++x<=XPerBucket; p++) {
            for (s=0, f=Filter; ++s<=NS; vp=(*vpp++)) {
                if (vp && !vp->flag.matte) {
                    if (vp->flag.opaque) {
                        for (j=0; ++j<=width; ) {
                            for (i=0; ++i<=width; ) {
                                p->r += *f * vp->color.r ;
                                p->g += *f * vp->color.g ;
                                p->b += *f * vp->color.b ;
                                p++->a += *f++ ;
                            }
                            p = (struct pixelrgba *)((char *)p+pskip) ;
                        }
                        p = (struct pixelrgba *)((char *)p-pback) ;
                    }
                    else {
                        alpha = 1. - (1./3.) *
                            (vp->trans.r+vp->trans.g+vp->trans.b);
                        for (j=0; ++j<=width; ) {
                            for (i=0; ++i<=width; ) {
                                p->r += *f * vp->color.r ;
                                p->g += *f * vp->color.g ;
                                p->b += *f * vp->color.b ;
                                p++->a += *f++ *alpha ;
                            }
                            p = (struct pixelrgba *)((char *)p+pskip) ;
                        }
                    }
                }
            }
        }
    }
}

```

```

        p = (struct pixelrba *)((char *)p-pback) ;
    }
    }
    else {
        f += fskip ;
    }
    }
}

```

...filter

```

float lerpz(v)
register struct xyz v[4] ;
{
/*
* Interpolate z using Shepard's method. Use the Manhattan distance
* to each vertex as an approximation to the actual distance.
*/
float alpha[4], dist[4], d01, d23 ;
float z ;
dist[0] = (v[0].x>0.) ? v[0].x : -v[0].x ;
dist[0] += (v[0].y>0.) ? v[0].y : -v[0].y ;
dist[1] = (v[1].x>0.) ? v[1].x : -v[1].x ;
dist[1] += (v[1].y>0.) ? v[1].y : -v[1].y ;
dist[2] = (v[2].x>0.) ? v[2].x : -v[2].x ;
dist[2] += (v[2].y>0.) ? v[2].y : -v[2].y ;
dist[3] = (v[3].x>0.) ? v[3].x : -v[3].x ;
dist[3] += (v[3].y>0.) ? v[3].y : -v[3].y ;
d01 = dist[0] * dist[1] ;
d23 = dist[2] * dist[3] ;
alpha[0] = d23 * dist[1] ;
alpha[1] = d23 * dist[0] ;
alpha[2] = d01 * dist[3] ;
alpha[3] = d01 * dist[2] ;
z = alpha[0] * v[0].z ;
z += alpha[1] * v[1].z ;
z += alpha[2] * v[2].z ;
z += alpha[3] * v[3].z ;
z /= alpha[0] + alpha[1] + alpha[2] + alpha[3] ;
Lerp++ ;
return z ;
}

```

lerpz

```

#if GOURAUD
gouraud(v,mp,vp)
register struct xyz v[4] ;
register struct mpoly *mp ;
register struct visiblepoint *vp ;
{
/*
* Interpolate using Shepard's method. Use the Manhattan distance
* to each vertex as an approximation to the actual distance.
*/
float alpha[4], sum, alphasum, dist[4], d01, d23 ;
dist[0] = (v[0].x>0.) ? v[0].x : -v[0].x ;
dist[0] += (v[0].y>0.) ? v[0].y : -v[0].y ;
dist[1] = (v[1].x>0.) ? v[1].x : -v[1].x ;
dist[1] += (v[1].y>0.) ? v[1].y : -v[1].y ;
dist[2] = (v[2].x>0.) ? v[2].x : -v[2].x ;
dist[2] += (v[2].y>0.) ? v[2].y : -v[2].y ;
dist[3] = (v[3].x>0.) ? v[3].x : -v[3].x ;
dist[3] += (v[3].y>0.) ? v[3].y : -v[3].y ;
d01 = dist[0] * dist[1] ;
d23 = dist[2] * dist[3] ;
alpha[0] = d23 * dist[1] ;
alpha[1] = d23 * dist[0] ;
alpha[2] = d01 * dist[3] ;
alpha[3] = d01 * dist[2] ;
alphasum = alpha[0] + alpha[1] + alpha[2] + alpha[3] ;
sum = alpha[0] * mp->color[0].r ;
sum += alpha[1] * mp->color[1].r ;

```

gouraud

```

sum += alpha[2] * mp->color[2].r ;
sum += alpha[3] * mp->color[3].r ;
vp->color.r = sum/alphasum ;
sum = alpha[0] * mp->color[0].g ;
sum += alpha[1] * mp->color[1].g ;
sum += alpha[2] * mp->color[2].g ;
sum += alpha[3] * mp->color[3].g ;
vp->color.g = sum/alphasum ;
sum = alpha[0] * mp->color[0].b ;
sum += alpha[1] * mp->color[1].b ;
sum += alpha[2] * mp->color[2].b ;
sum += alpha[3] * mp->color[3].b ;
vp->color.b = sum/alphasum ;
sum = alpha[0] * mp->trans[0].r ;
sum += alpha[1] * mp->trans[1].r ;
sum += alpha[2] * mp->trans[2].r ;
sum += alpha[3] * mp->trans[3].r ;
vp->trans.r = sum/alphasum ;
sum = alpha[0] * mp->trans[0].g ;
sum += alpha[1] * mp->trans[1].g ;
sum += alpha[2] * mp->trans[2].g ;
sum += alpha[3] * mp->trans[3].g ;
vp->trans.g = sum/alphasum ;
sum = alpha[0] * mp->trans[0].b ;
sum += alpha[1] * mp->trans[1].b ;
sum += alpha[2] * mp->trans[2].b ;
sum += alpha[3] * mp->trans[3].b ;
vp->trans.b = sum/alphasum ;

```

```

}
#endif GOURAUD

```

```

static sample (nsample, mp, v)

```

sample

```

    int nsample ;
    register struct mpoly *mp ;
    register struct xyz v[4] ;

    {
        register struct visiblepoint *vp ;
        register int inside ;
        float z ;

```

```

/* If the micropolygon crosses the hither or yon plane during this
 * frame, see if it crosses it for this sample
 */

```

```

#if MOTIONBLUR && IGLOSS
    If (mp->flag.hitheryoncrossing && mp->flag.moving) {
        float zmin, zmax ;
        If (v[0].z < v[1].z) {
            If (v[2].z < v[3].z) {
                zmin = (v[0].z < v[2].z) ? v[0].z : v[2].z ;
                zmax = (v[1].z > v[3].z) ? v[1].z : v[3].z ;
            }
            else {
                zmin = (v[0].z < v[3].z) ? v[0].z : v[3].z ;
                zmax = (v[1].z > v[2].z) ? v[1].z : v[2].z ;
            }
        }
        else {
            If (v[2].z < v[3].z) {
                zmin = (v[1].z < v[2].z) ? v[1].z : v[2].z ;
                zmax = (v[0].z > v[3].z) ? v[0].z : v[3].z ;
            }
            else {
                zmin = (v[1].z < v[3].z) ? v[1].z : v[3].z ;
                zmax = (v[0].z > v[2].z) ? v[0].z : v[2].z ;
            }
        }
        If (zmin < Hither || zmax > Yon) goto Outside ;
    }
#endif MOTIONBLUR && IGLOSS

```

```

/*
 * The inside test has been unrolled for speed. This test usually takes
 * 6 comparisons and branches, 4 multiplications, and 1-3 assignments.

```


...sample

- * > If vertices 0 and 2 have different y signs, then both
- * > The line from vertex 1 to either vertex 0 or vertex 2 crosses the z axis, depending on the sign of vertex 1.
- * > The line from vertex 3 to either vertex 0 or vertex 2 crosses the z axis, depending on the sign of vertex 3.
- * > Otherwise, if vertices 0 and 2 have the same sign, then
- * > The lines from vertex 1 to vertex 0 and vertex 2 either both cross the z axis or both do not cross the z axis, depending on the sign of vertex 1.
- * > The lines from vertex 3 to vertex 0 and vertex 2 either both cross the z axis or both do not cross the z axis, depending on the sign of vertex 3.
- * For every line that crosses the z axis, we test the sign of the crossing
- * and toggle "inside" if the crossing is positive. At the end, "inside" is
- * set iff we encountered an odd number of positive z crossings.

```

/*
inside = 0 ;
If (v[0].y > 0.0) {
  If (v[2].y < 0.0) {
    If (v[1].y < 0.0)
      { If (v[1].x*v[0].y > v[1].y*v[0].x) inside = ~inside; }
      else
        { If (v[2].x*v[1].y > v[2].y*v[1].x) inside = ~inside; }
    If (v[3].y < 0.0)
      { If (v[3].x*v[0].y > v[3].y*v[0].x) inside = ~inside; }
      else
        { If (v[2].x*v[3].y > v[2].y*v[3].x) inside = ~inside; }
  }
  else {
    If (v[1].y < 0.0) {
      If (v[1].x*v[0].y > v[1].y*v[0].x) inside = ~inside;
      If (v[1].x*v[2].y > v[1].y*v[2].x) inside = ~inside;
    }
    If (v[3].y < 0.0) {
      If (v[3].x*v[0].y > v[3].y*v[0].x) inside = ~inside;
      If (v[3].x*v[2].y > v[3].y*v[2].x) inside = ~inside;
    }
  }
}
else {
  If (v[2].y > 0.0) {
    If (v[1].y > 0.0)
      { If (v[1].x*v[0].y < v[1].y*v[0].x) inside = ~inside; }
      else
        { If (v[2].x*v[1].y < v[2].y*v[1].x) inside = ~inside; }
    If (v[3].y > 0.0)
      { If (v[3].x*v[0].y < v[3].y*v[0].x) inside = ~inside; }
      else
        { If (v[2].x*v[3].y < v[2].y*v[3].x) inside = ~inside; }
  }
  else {
    If (v[1].y > 0.0) {
      If (v[1].x*v[0].y < v[1].y*v[0].x) inside = ~inside;
      If (v[1].x*v[2].y < v[1].y*v[2].x) inside = ~inside;
    }
    If (v[3].y > 0.0) {
      If (v[3].x*v[0].y < v[3].y*v[0].x) inside = ~inside;
      If (v[3].x*v[2].y < v[3].y*v[2].x) inside = ~inside;
    }
  }
}
}
}

```

- * If the sample point is inside the polygon, and the micropolygon
- * crosses the hither or yon plane, interpolate to find the value of
- * z at the sample point. Test whether this z is between the hither
- * and yon planes.

```

/*
If (!inside) goto Outside ;

If (mp->flag.hitheryoncrossing) {
  z = lerpz (v) ;
  If (z < Hither || z > Yon) goto Outside ;
}

```

```

If (!VisFreeList) {
    int vismallocated, i ;
    VisFreeList = (struct visiblepoint *) malloc ((unsigned)VisMallocSize) ;
    vismallocated = VisMallocSize/sizeof(struct visiblepoint) ;
    NVis += vismallocated ;
    for (j=1, vp=VisFreeList; i<vismallocated; vp++, i++) {
        vp->next = vp+1 ;
    }
    vp->next = 0 ;
}

vp = VisFreeList ;
VisFreeList = VisFreeList->next ;
NVisUse++ ;
If (NVisUse>NVisMaxUsed) NVisMaxUsed=NVisUse ;

#ifdef CSG
vp->csgtree = mp->csgtree ;
vp->csgnode = mp->csgnode ;
#endif CSG
vp->glassbackopacity = mp->glassbackopacity ;
vp->flag = mp->flag ;
If (mp->flag.bitheryoncrossing) {
    vp->minz = z ;
    vp->maxz = z ;
    vp->flag.lerpdone = 1 ;
}
else {
    vp->minz = mp->minz ;
    vp->maxz = mp->maxz ;
    vp->flag.lerpdone = 0 ;
}
bcopy ((char *)v,(char *)vp->v,sizeof(vp->v)) ;
#ifdef GOURAUD
If (mp->flag.gouraud)
    gouraud (v,mp,vp) ;
else {
    vp->color = mp->color[0] ;
    vp->trans = mp->trans[0] ;
}
else
    vp->color = mp->color ;
    vp->trans = mp->trans ;
#endif GOURAUD
vp->next = Point[nsample] ;
i'oint[nsample] = vp ;
llit++ ;
return ;

Outside:
Miss++ ;
return ;

/* bit reversal, but mapped back onto 0-n */
permute(i,n) {
    register int j,a,b;
    j=0;
    for(b=1;b+b<n;b+=b) ;
    for(a=1;a>=1;a+=a,b/=2)
        If (i-b>=0) {i-=b; j+=a;}
    If (j>=n) j=a+1-j;
    return j;
}

tablesinit(nx,ny) {
    register int i, j, s ;
    int x, y, t, f ;
    float dx, dy, dt, sum ;
    int width ;

    NS = nx*ny;
    SamplesPerBucket = PixelsPerBucket * NS ;
    width = 1 + 2 * Border ;

```

...sample

permute

tablesinit

```

/* malloc room for tables */
If (Location) free((char *)Location) ;
If (Filter) free((char *)Filter) ;
If (Lens) free((char *)Lens) ;
Location = (struct xy *)malloc(NS*sizeof(struct xy)) ;
Filter = (float *)malloc(NS*width*width*sizeof(float)) ;
Lens = (struct xy *)malloc(NS*sizeof(struct xy)) ;

/* Calculate table of random numbers */
If (JitterFlag) {
    MaxXJitter = 1./nx;
    MaxYJitter = 1./ny;
    for (s=0; s<NJITTER; s++) {
        XJitter[s] = drand()/nx ;
        YJitter[s] = drand()/ny ;
        TJitter[s] = drand()/NS ;
        LXJitter[s] = drand()/nx ;
        LYJitter[s] = drand()/ny ;
    }
    MaxXJitter -= (float)0.999999 ;
    MaxYJitter -= (float)0.999999 ;
}
else {
    MaxXJitter = 0.5/nx;
    MaxYJitter = 0.5/ny;
    for (s=0; s<NJITTER; s++) {
        XJitter[s] = 0.5/nx ;
        YJitter[s] = 0.5/ny ;
        TJitter[s] = 0.5/NS ;
        LXJitter[s] = 0.5/nx ;
        LYJitter[s] = 0.5/ny ;
    }
    MaxXJitter -= (float)0.999999 ;
    MaxYJitter -= (float)0.999999 ;
}

/* Calculate locations */
for (s=0, x=0; x<nx; x++) {
    for (y=0; y<ny; y++, s++) {
        t=permute(s,NS);
        Location[t].x = x / (float)nx ;
        Location[t].y = y / (float)ny ;
    }
}

/* Create filter table. */
/* Calculate filter values for the center of each sampling region. */
sum = 0.0 ;
for (s=0, f=0; s<NS; s++) {
    for (j=0; j<width; j++) {
        for (i=0; i<width; i++, f++) {
            dx = Location[s].x + 0.5/nx - (i - Border +.5) ;
            dy = Location[s].y + 0.5/ny - (j - Border +.5) ;
            Filter[f] = (*FilterRoutine[FilterType])(dx,dy) ;
            sum += Filter[f] ;
        }
    }
}

/* Normalize filter */
for (i=0; i<NS*width*width; i++)
    Filter[i] /= sum ;

/* Lens. This is a kludge for now - uses a square lens */
for (s=0; s<NS; s++) {
    Lens[s].x = Location[s].x ;
    Lens[s].y = Location[s].y ;
}
}

```

```

static freelist (vp)
  register struct visiblepoint *vp ;
{
  register struct visiblepoint *p ;
  register int n ;

  if (!vp) return ;
  for (p=vp, n=1; p->next; n++, p=p->next) ;
  p->next = VisFreeList ;
  NVisInUse -- n ;
  VisFreeList = vp ;
}

```

freelist

```

static freepoints()
{
  register int n ;
  register struct visiblepoint **head ;
  for (n=0, head=Point; n<SamplesPerBucket; head++, n++) {
    freelist (*head) ;
  }
}

```

freepoints

```

#if CSG
/*----- CSG code -----*/

```

```

#define CSGDifferenceOp 1
#define CSGIntersectionOp 2
#define CSGUnionOp 3

```

```

#define MAXTREE 64
static struct CSGnode *Tree[MAXTREE];

```

```

static int CSGNewTree(n,tree)
  int n;
  struct CSGnode *tree;
{
  if (n>=MAXTREE) {
    fprintf (stderr, "Maximum number of trees exceeded.\n");
    Error();
    return;
  }
  Tree[n] = tree;
}

```

CSGNewTree

```

static int CSGResolve()
{
  int ntree ;
  register int n ;
  register struct visiblepoint **vp ;
  register struct visiblepoint *resolvedlist, *front, *vis ;
  struct visiblepoint *treelist ;
  struct visiblepoint *extract_csgtree(), *mergelists();
  struct visiblepoint *extract_csgnode(), *sortfront() ;

  for (n=0, vp=Point; n<SamplesPerBucket; vp++, n++) {
    vis = 0 ;
    while (front=sortfront(vp)) {
      if (front->flag.pantshack) {
        *vp = front->next ;
        front->next = 0 ;
        freelist(front) ;
        front = sortfront(vp) ;
      }
      if (front && front->flag.torsohack) {
        *vp = front->next ;
        front->next = 0 ;
        freelist(front) ;
      }
    }
  }
}

```

CSGResolve

```

else if (front->csgnode) {
    ntree = front->csgtree ;
    treelist = extract_csgtree (ntree, vp) ;
    csg_resolve_tree (Tree[ntree], 0, &treelist) ;
    resolvedlist = extract_csgnode (0, &treelist) ;
    freelist ( treelist ) ;
    *vp = mergelists (resolvedlist,*vp) ;
}
else {
    *vp = front->next ;
    if (vis) {
        front->color.r *= vis->trans.r ;
        front->color.g *= vis->trans.g ;
        front->color.b *= vis->trans.b ;
        front->color.r += vis->color.r ;
        front->color.g += vis->color.g ;
        front->color.b += vis->color.b ;
        front->trans.r *= vis->trans.r ;
        front->trans.g *= vis->trans.g ;
        front->trans.b *= vis->trans.b ;
    }
    front->next = vis ;
    vis = front ;
    if (vis->flag.glasshack && *vp) {
        float alpha, comp ;
        front = sortfront(vp) ;
        alpha = vis->glasshackopacity ;
        comp = vis->color.r ;
        vis->color.r *= alpha ;
        vis->color.r += (1-alpha) * comp * front->color.r ;
        comp = vis->color.g ;
        vis->color.g *= alpha ;
        vis->color.g += (1-alpha) * comp * front->color.g ;
        comp = vis->color.b ;
        vis->color.b *= alpha ;
        vis->color.b += (1-alpha) * comp * front->color.b ;
    }
    if (vis->flag.opaque) break ;
}
}
*vp = mergelists (vis, *vp) ;
}
}

```

```

static csg_resolve_surface (lista, listb, id, op)
register struct visiblepoint *lista, *listb ;
int id, op ;
{
    register int a, b ;

```

csg_resolve_surface

```

/* Go through two sorted lists of points, determining which points are
 * actually on the surface according to the specified csg operator.
 * Mark the points that are on the surface with the specified node id.
 * A point from listb is on the surface if "a" is set; a point from
 * lista is on the surface if "b" is set.
 * > For the union operator, accept points from lista iff we are outside
 * of volume b, and accept points from listb iff we are outside of
 * volume a. Since we are initially outside of both volumes, "a" and
 * "b" are both initially true.
 * > For the intersection operator, accept points from one list iff we
 * are inside the other volume. Since we are initially not inside
 * either volume, "a" and "b" are both initially false.
 * > For the difference operator (a minus b), accept points from lista
 * iff we are outside of volume b, and accept points from listb iff
 * we are inside volume a. Since we are initially outside of b and
 * not inside a, "b" is initially true and "a" is initially false.
 * > For all three operators, toggle "a" or "b" when we pass through
 * one of the surfaces of a or b, respectively.
 */
a = b = 0 ;
switch (op) {

```

```

case CSGUnionOp:      a = `a ;
case CSGDifferenceOp: b = `b ;
case CSGIntersectionOp: break ;
}

while (lista && listb) {
  if (lista->minz < listb->minz) {
    if (b) lista->csgnode = id ;
    lista = lista->next ;
    a = `a ;
  }
  else {
    if (a) listb->csgnode = id ;
    listb = listb->next ;
    b = `b ;
  }
}
if (b)
  for (; lista; lista = lista->next) lista->csgnode = id ;
if (a)
  for (; listb; listb = listb->next) listb->csgnode = id ;
}

```

```

static struct visiblepoint *extract_csgnode (nodeid, list)
  int nodeid ;
  register struct visiblepoint **list ;
{
  register struct visiblepoint *thisid, *notthisid, *vp, *next ;

```

extract_csgnode

```

/* Extract all points with the specified node number from the list.
 * Return a pointer to the head of a new list containing only the
 * extracted points.
 */

```

```

thisid = 0 ;
notthisid = 0 ;
next = *list ;
while (vp = next) {
  next = vp->next ;
  if (vp->csgnode == nodeid) {
    vp->next = thisid ;
    thisid = vp ;
  }
  else {
    vp->next = notthisid ;
    notthisid = vp ;
  }
}
*list = notthisid ;
return thisid ;
}

```

```

static struct visiblepoint *extract_csgtree (ntree, list)
  int ntree ;
  register struct visiblepoint **list ;
{
  register struct visiblepoint *intree, *notinntree, *vp, *next ;

```

extract_csgtree

```

intree = notintree = 0 ;
vp = *list ;
while (vp) {
  next = vp->next ;
  if (vp->csgtree == ntree) {
    vp->next = intree ;
    intree = vp ;
  }
  else {
    vp->next = notintree ;
    notintree = vp ;
  }
}

```

```

    }
    vp = next ;
}

*list = notintree ;
return intree ;
}

```

```

static struct visiblepoint *findfront(list)
    register struct visiblepoint *list;
{
    register struct visiblepoint *front, *vp ;

```

findfront

```

/* This routine returns a pointer to the frontmost point of a list
 * of visiblepoints. The z value of each point is stored as the
 * minimum and maximum z values of its micropolygon. The exact
 * z value is only calculated (by interpolation) if it is needed.
 * The exact value is stored in both the minimum and maximum z fields.
 * > Find the point 'front' with the smallest minimum z.
 * > If that point has an interpolated z value, we're done.
 * > If that point's maximum z value is in front of the minimum z
 * of every other point, we're done.
 * > Otherwise we go through the list again, this time using the
 * exact values of z calculated by interpolation.
*/

```

...findfront

```

    If (!list) return 0 ;

    for (front=vp=list; vp; vp=vp->next)
        If (vp->minz < front->minz)
            front = vp ;

    If (front->flag.lerpdone) goto Done ;

    for (vp=list; vp; vp=vp->next)
        If (vp!=front && vp->minz < front->maxz) goto Lerp;
    goto Done;

Lerp:
    front->minz = front->maxz = lerpz(front->v) ;
    front->flag.lerpdone = 1 ;
    for (vp=list; vp; vp=vp->next) {
        If (vp->minz < front->minz) {
            If (vp->flag.lerpdone)
                front = vp ;
            else {
                vp->minz = vp->maxz = lerpz(vp->v) ;
                vp->flag.lerpdone = 1 ;
                If (vp->minz < front->minz)
                    front = vp ;
            }
        }
    }

Done:
    return front ;
}

```

```

static struct visiblepoint *mergelists(a,b)
    register struct visiblepoint *a, *b ;
{
    register struct visiblepoint *p ;

```

mergelists

```

    If (!a) return b ;
    If (!b) return a ;

    for (p=a; p->next; p=p->next) ;
    p->next = b ;
    return a;
}

```

```

static csg_resolve_tree (node, id, list)
  register struct CSGnode *node ;
  int id ;
  register struct visiblepoint **list ;
{
  struct visiblepoint *list0, *list1 ;
  struct visiblepoint *extract_csgnode(), *mergelists() ;

  If (node->child[0]) csg_resolve_tree (node->child[0], node->id[0], list);
  If (node->child[1]) csg_resolve_tree (node->child[1], node->id[1], list);
  list0 = extract_csgnode (node->id[0], list) ;
  list1 = extract_csgnode (node->id[1], list) ;
  If (list0 || list1) {
    If (list0) sortlist (&list0) ;
    If (list1) sortlist (&list1) ;
    csg_resolve_surface (list0, list1, id, node->op) ;
    *list = mergelists (list0,*list) ;
    *list = mergelists (list1,*list) ;
  }
}

```

csg_resolve_tree

```

static struct visiblepoint *sortfront(head)
  register struct visiblepoint **head;
{
  register struct visiblepoint *prev, *temp, *vp, *front ;
/*
 * (*head) points to a list of visible points. This routine puts
 * the frontmost point at the head of the list.
 */
  If (!*head) return 0 ;
  front = findfront(*head) ;
  for (prev = *head, vp = prev->next; vp; prev = vp, vp = vp->next) {
    If (vp == front) {
      prev->next = front->next ;
      front->next = *head ;
      *head = front ;
      return *head ;
    }
  }
  return *head ;
}

```

sortfront

```

static sortlist (list)
  register struct visiblepoint **list ;
{
  If ((*list)->next) {
    (void) sortfront (list) ;
    sortlist (&((*list)->next)) ;
  }
}

```

sortlist

```

#else
static int CSGNewTree();
static int CSGResolve();
#endif CSG
/* asvis.h 1.9 85/05/20 */

```

CSGNewTree
CSGResolve

```

#include <reves.h>

struct visflag {
  unsigned moving : 1 ;
  unsigned opaque : 1 ;
  unsigned cubicmotion : 1 ;
  unsigned matte : 1 ;
  unsigned hitheryoncrossing : 1 ;
  unsigned lepdone : 1 ;
  unsigned gouraud : 1 ;
  unsigned pantshack : 1 ;
  unsigned torsoback : 1 ;
  unsigned glassback : 1 ;
};

```



```

struct mpoly {
    struct mpoly *next ;
    int minx, miny, maxx, maxy ;
    struct xyz min, max ;
    struct xyz v[4] ;
#ifdef MOTIONBLUR
    struct xyz speed[4] ;
#endif
#ifdef CUBICMOTION
    struct xyz speed2[4] ;
    struct xyz speed3[1] ;
#endif
#ifdef MOTIONBLUR
#endif
#ifdef GOURAUD
    struct color color[4] ;
    struct color trans[4] ;
#else
    struct color color ;
    struct color trans ;
#endif
#ifdef CSG
    short csgtree, csgnode ;
#endif
#ifndef CSG
    /* DEPTHOFIELD
    struct xy dofborder ;
#endif
    float glashackopacity ;
    struct visflags flag ;
};

extern float Dofx_a, Dofx_b, Dofy_a, Dofy_b ;
extern int PinholeCamera ;

```

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APPENDIX B

/u0/tom/patent/pray.c

/u0/tom/patent/pray.c

...lighthit

```

    if (hitlight != NULL)
        return(hitalpha);
    return(-f.);
}

```

disperseray(olddray,maxdispersionangle)

disperseray

```

vector olddray;
double maxdispersionangle;
{
    double phi,theta,rho;
    double a,b,c,v,x,y,z;
    phi = drand()*drand()*maxdispersionangle;
    theta = drand()*2*PI;
    a = olddray[0];
    b = olddray[1];
    c = olddray[2];
    rho = sqrt((double)(a*a+b*b+c*c));
    a = a/rho; b = b/rho; c = c/rho;
    x = rho*sin(phi)*cos(theta);
    y = rho*sin(phi)*sin(theta);
    z = rho*cos(phi);
    if ((v = sqrt((double)(b*b+c*c))) != 0)
    {
        olddray[0] = (x*v + z*a);
        olddray[1] = (y*v - b*a*a + b*a*v)/v;
        olddray[2] = (-b*v - c*a*a + c*a*v)/v;
    }
    else
    {
        olddray[0] = z*a;
        olddray[1] = y;
        olddray[2] = -x*a;
    }
}
struct color

```

```

trace(viewing, level,time)
register struct ray viewing;
float time;

```

trace

```

{
    double alpha,beta;
    struct ray newray;
    double diffuse, vdotn, kf, kn, specular, reflectionlength;
    struct color tracecolor, viewcolor, spherecolor;
    double spherereflectivity,spherebump;
    vector normal, incoming, reflection, tempvect, center;
    double radius;
    register struct sphere hp;
    register struct light lptr;
    matrix tempmatrix;
    double spinangle;

/*print("trace(ray: %f, %f, %f, %f, %f, %f), %d, %f)\n",
viewing->endpoint[0],
viewing->endpoint[1],
viewing->endpoint[2],
viewing->direction[0],
viewing->direction[1],
viewing->direction[2],
level,time);*/

    alpha = spherehit(viewing,time,(level==0) && !translucencyray);
    beta = lighthit(viewing,time);
    if ((beta >= 0) && ((alpha < 0) || (beta < alpha)))
        return(hiligh->rgb);
    if (alpha < 0.)
        return(nulcolor);
    viewcolor.red =
    viewcolor.grn =
    viewcolor.blu = 0;
    viewcolor.alf = 1.;
    hp = hitsphere;
    VzAddLerp(alpha,viewing->endpoint,viewing->direction,newray.endpoint);

    FindCenter(hp,time,center);
    radius = hp->radius;

    normal[0] = (newray.endpoint[0]-center[0])/radius;
    normal[1] = (newray.endpoint[1]-center[1])/radius;
    normal[2] = (newray.endpoint[2]-center[2])/radius;
    normal[3] = 1.;

/*
put normal through inverse transformation in order to extract
original position on sphere.

that original position is then used to look up the parameters
for the sphere
*/
{
    double duration;
    struct movement mptr;

    mptr = hp->mptr;
    VzCopy(normal,tempvect);
    MxVectorMultiply(tempvect,hp->M,tempvect);
    while (mptr)
    {
        if (mptr->starttime >= time) break;
        MxVectorMultiply(tempvect,mptr->MR1MR2,tempvect);
        if (mptr->mptr)
            if (mptr->mptr->starttime >= time)
                duration = time - mptr->starttime;
            else
                duration = mptr->mptr->starttime - mptr->starttime;
        else
            duration = time - mptr->starttime;
        spinangle = MxDegree(duration * VzLength(mptr->translate)/hp->radius);
        MxRotate(spinangle, 's', tempmatrix);
        MxVectorMultiply(tempvect,tempmatrix,tempvect);
        MxVectorMultiply(tempvect,mptr->IR2IR1,tempvect);
        mptr = mptr->mptr;
    }
}

/*
now tempvect contains the original position of this endpoint in the
picture map for this sphere.
*/
    spherebump = hp->phong;
    if (ABS(tempvect[2]) < halfstripwidth)

```

```

        {
            spherecolor = hp->atripecolor;
            sphererefectivity = spherecolor.alf;
        }
    else
        if ((ABS(tempvect[2]) < halfringwidth))
            {
/*% cc -g -s % cook.o boundsphere.o -lG -lrpc -lpicio -ltp -las -lmx -lsm -lm
*/
#include <stdio.h>
#include <aarg.h>
#include <math.h>
#include <picio.h>
#include <rpc.h>
#include <ikehack.h>
#include <bliss.h>
#include <MzMatrix.h>
#include <BuniOpen.h>

#include <rand.h>

#include <VsVector.h>

#define SS 84
#define XSIZE 512
#define YSIZE 488

int spx = XSIZE;
int spy = YSIZE;
int ppfx = XSIZE;
int ppy = YSIZE;
int pps = 1;
int size = 0;
int rpp = SS;

#define VPIX .7868252459 /* = 48/61, vertical height of a pixel of
#define MAXLEVEL 1
#define NSPHERE 100

int translucencyray = FALSE;

double fieldofview = 30;
vector viewpoint;
matrix normaliser,inversenormaliser;

double halfstripewidth = .4722;
double halfringwidth = .85;
double linethickness = .05;
double ringradius = .44;
/* ringradius = sqrt(1-(halfringwidth+linethickness)*2) */

int dms = 0;

int ystart = 0;
int yend = 100000;
setystart()
    {
        ystart = atoi(aargv[1]);
        yend = atoi(aargv[2]);
        if (yend < ystart)
            {
                fprintf(stderr,"bad y bounds\n");
                exit(1);
            }
    }

int debug = FALSE;
setdebug() {debug = TRUE;}

struct color
    {
        double red, grn, blu, alf;
    };
struct color nullcolor = {0.,0.,0.,0.};
struct color ivorycolor = {0.85,0.85,0.55,0.8};
double ivorybump = 1000.;
double ivoryreflectivity = 0.8;
struct color blackcolor = {0.05,0.05,0.05,1.};
double blackbump = 1000.;
double blackreflectivity = 0.8;

struct window {int minx,maxx,miny,maxy;};

struct movement
    {
        matrix MR1MR2,IR2IR1;
        double starttime;
        vector translate;
    }

```

...trace

setystart

setdebug

```

    struct movement *mptr;
};
struct sphere
{
    vector center;
    double radius;
    matrix M;
    struct color outsidecolor,stripcolor;
    struct movement *mptr;
    double refractiveindex; /* refractive index */
    double transmissivity; /* fractional intensity of transmitted rays */
    double specularity; /* amount of specular reflection */
    double phong; /* specular bump width (Phong exponent) */
    double reflectiondispersion;
    double transmissiondispersion;
    int active;
    struct window w;
    BuniPtrType buniptr;
    int fbxsize,fbysize;
}
sphere[NSPIHERE];

struct sphere *sphere = sphere;

#define NLIGHT 50
struct light
{
    vector location0;
    double intensity0;
    vector location1;
    double intensity1;
    double radius;
    struct color rgb;
}
light[NLIGHT];

struct light *light = light;

double ambient;

struct ray
{
    vector endpoint,direction;
};

struct sphere *hitsphere;
struct light *hitlight;
#define EPSILON 1e-6

FindCenter(sptr,time,center)
struct sphere *sptr;
double time;
vector center;
{
    double duration;
    struct movement *mptr;

    VxCopy(sptr->center,center);
    mptr = sptr->mptr;
    while (mptr)
    {
        if (mptr->starttime >= time) break;
        if (mptr->mptr)
            if (mptr->mptr->starttime >= time)
                duration = time - mptr->starttime;
            else
                duration = mptr->mptr->starttime - mptr->starttime;
        else
            duration = time - mptr->starttime;
        VxAddLerp(duration,center,mptr->translate,center);
        mptr = mptr->mptr;
    }
}

double
sphererhit(olddray,time,level0)
register struct ray *olddray;
float time;
{
    register struct sphere *mptr;
    double hitalpha;
    double alpha,discriminant,a,b,c;
    vector newendpoint;
    vector center;
    double radius;
}

```

*FindCenter**sphererhit*

```

/printf(" spherehit(ray:(%f,%f,%f),%f,%f,%f),%f)\n",
oldray->endpoint[0],oldray->endpoint[1],oldray->endpoint[2],
oldray->direction[0],oldray->direction[1],oldray->direction[2],time);*/

```

```

/* This routine tries to find a point on the sphere sptr and the oldray.
Using alpha as the extent of the ray beyond oldray->endpoint,
a quadratic in alpha can be formed whose coefficients a, b, c are
as computed below.
*/

```

```

hitsphere = NULL;
a = VxDot(oldray->direction,oldray->direction);
for (sptr = sphere; sptr != esphere; sptr++)
{
    if (!level0 || sptr->active)
    {
        FindCenter(sptr,time,center);
        radius = sptr->radius;

        VxSubtract(oldray->endpoint,center,newendpoint);
        b = 2*VxDot(newendpoint,oldray->direction);
        c = VxDot(newendpoint,newendpoint)-radius*radius;
        if ((discriminant = b*b - 4*a*c) < 0.)
            continue;

        discriminant = sqrt((double)discriminant);

        alpha = (-b+discriminant)/(2*a);
        if (EPSILON < alpha &&
            (hitsphere == NULL || alpha < hitalpha))
            {
                hitalpha = alpha;
                hitsphere = sptr;
            }

        alpha = (-b-discriminant)/(2*a);
        if (EPSILON < alpha &&
            (hitsphere == NULL || alpha < hitalpha))
            {
                hitalpha = alpha;
                hitsphere = sptr;
            }
    }
}
if (hitsphere != NULL)
    return(hitalpha);
return(-1.);
}

```

...spherehit

```

double
lighthit(oldray,time)
register struct ray *oldray;
float time;

```

```

{
    register struct light *lptr;
    double hitalpha;
    double alpha, discriminant, a, b, c;
    vector newendpoint;
    vector center;
    double radius;

    hitlight = NULL;
    a = VxDot(oldray->direction,oldray->direction);
    for (lptr = light; lptr != elight; lptr++)
    {
        VxLerp(time,lptr->location0,lptr->location1,center);
        radius = lptr->radius;
        VxSubtract(oldray->endpoint,center,newendpoint);
        b = 2*VxDot(newendpoint,oldray->direction);
        c = VxDot(newendpoint,newendpoint)-radius*radius;
        if ((discriminant = b*b - 4*a*c) < 0.)
            continue;

        discriminant = sqrt((double)discriminant);

        alpha = (-b+discriminant)/(2*a);
        if (EPSILON < alpha &&
            (hitsphere == NULL || alpha < hitalpha))
            {
                hitalpha = alpha;
                hitlight = lptr;
            }

        alpha = (-b-discriminant)/(2*a);
        if (EPSILON < alpha &&
            (hitsphere == NULL || alpha < hitalpha))

```

lighthit

```

        hitalpha = alpha;
        highlight = lptr;
    }
}
...trace

    spherecolor = hp->outsidecolor;
    spherereflectivity = spherecolor.alf;
}
else
    if (ABS(tempvect[2]) < halfringwidth+linethickness)
    {
        if (hp->outsidecolor.red != hp->stripecolor.red)
        {
            spherecolor = blackcolor;
            spherereflectivity = blackreflectivity;
            spherebump = blackbump;
        }
        else
        {
            spherecolor = ivorycolor;
            spherereflectivity = ivoryreflectivity;
            spherebump = ivorybump;
        }
    }
else
    if (hp->buniptr)
    {
        int mapx,mapy;
        RGBA*ixelType RGBA;

        {
            if (tempvect[2] > 0)
            {
                mapx = hp->fbssize*(1 + (atan(tempvect[0]/tempvect[2])/(PI/2))/ringradius)/2;
                mapy = hp->fbssize*(1 - (atan(tempvect[1]/tempvect[2])/(PI/2))/ringradius)/2;
            }
            else
            {
                mapx = hp->fbssize*(1 + (atan(tempvect[0]/tempvect[2])/(PI/2))/ringradius)/2;
                mapy = hp->fbssize*(1 - (atan(tempvect[1]/tempvect[2])/(PI/2))/ringradius)/2;
            }

            SetBunIY(hp->buniptr,mapy);
            SetBunIX(hp->buniptr,mapx);
            GetBunI_RGBA(hp->buniptr,&RGBA);
            spherecolor.red = RGBA.Red /4095.;
            spherecolor.grn = RGBA.Green /4095.;
            spherecolor.blu = RGBA.Blue /4095.;
            spherereflectivity = RGBA.Alpha/4095.;
            spherebump = 1000;
        }
    }
else
    {
        spherecolor = ivorycolor;
        spherereflectivity = ivoryreflectivity;
        spherebump = ivorybump;
    }

    vdotn = VzDot(normal,viewing->direction);
    if (vdotn > 0.)
    {
        VxNegate(normal,normal);
        kn = 1./hp->refractiveindex;
    }
else
    {
        vdotn = -vdotn;
        kn = hp->refractiveindex;
    }
}
...trace

    if(vdotn != 0.)
        VxScalarMultiply(1/vdotn,viewing->direction,incoming);
    /* the only difference between the viewing direction and the incoming
       vector is this factor of 1/vdotn, 1 over the sin of the angle
       between the viewing vector and the normal
    */
    if (vdotn == 0.)
        VxCopy(viewing->direction,reflection);
    else
        VxAddLerp(2.,incoming,normal,reflection);

    disperserny(reflection,hp->reflectiondispersion);

    reflectionlength = VzLength(reflection);

```

```

/*
 * first, get the lightsource components
 */
viewcolor.red = spherecolor.red * ambient;
viewcolor.grn = spherecolor.grn * ambient;
viewcolor.blu = spherecolor.blu * ambient;

for (lptr = light; lptr != elight; lptr++)
{
    double intensity;
    vector lightcenter;
    vector random;
    random[3] = 1;
    for (;;)
    {
        random[0] = 2 * drand() - 1;
        random[1] = 2 * drand() - 1;
        random[2] = 2 * drand() - 1;
        if (VxLength(random) <= 1) break;
    }
    VxScalarMultiply(lptr->radius, random, random);

    VxLerp(time, lptr->location0, lptr->location1, lightcenter);
    VxAdd(lightcenter, random, newray.direction);
    VxSubtract(newray.direction, newray.endpoint, newray.direction);
    VxNormalise(newray.direction, newray.direction);

    if (spherehit(&newray, time, FALSE) > 0.)
        continue;
    specular = VxDot(newray.direction, reflection) / reflectionlength;
    if (specular < 0.) specular = 0.;
    /*
     * Plastic alert
     */
    intensity = lptr->intensity0 + time * (lptr->intensity1 - lptr->intensity0);
    specular = hp->specularity * pow(specular, spherebump);
    diffuse = intensity * VxDot(newray.direction, normal);
    viewcolor.red += specular + diffuse * spherecolor.red;
    viewcolor.grn += specular + diffuse * spherecolor.grn;
    viewcolor.blu += specular + diffuse * spherecolor.blu;
}

if (level == MAXLEVEL)
    return(viewcolor);
/*
 * Now, the reflected component
 */
if (sphererefractivity != 0.)
    ...trace
    {
        double expf, alpha;
        VxCopy(reflection, newray.direction);
        tracecolor = trace(&newray, level+1, time);
        viewcolor.red += tracecolor.red * sphererefractivity;
        viewcolor.grn += tracecolor.grn * sphererefractivity;
        viewcolor.blu += tracecolor.blu * sphererefractivity;
    }
/*
 * if ((alpha = spherehit(&newray, time, FALSE) * VxLength(newray.direction)) > 0)
{
    viewcolor.red -= spherecolor.red * ambient * sphererefractivity * exp(-alpha);
    viewcolor.grn -= spherecolor.grn * ambient * sphererefractivity * exp(-alpha);
    viewcolor.blu -= spherecolor.blu * ambient * sphererefractivity * exp(-alpha);
}
/*
 * Now, the transmitted component
 */
if (hp->transmittivity != 0. && vdotn != 0.)
{
    VxAdd(incoming, normal, tempvect);
    kf = kn * kn * VxDot(incoming, incoming) - VxDot(tempvect, tempvect);
    if (kf > 0.)
    {
        kf = 1. / sqrt((double)kf);
        newray.direction[0] = kf * (normal[0] + incoming[0]) - normal[0];
        newray.direction[1] = kf * (normal[1] + incoming[1]) - normal[1];
        newray.direction[2] = kf * (normal[2] + incoming[2]) - normal[2];
        newray.direction[3] = 1.;
    }

    disperseray(newray.direction, hp->transmissiondispersion);
}

/* print out trace ray: (x0, x1, x2, x3, x4, x5) -> */

```

```

newray.endpoint[0],
newray.endpoint[1],
newray.endpoint[2],
newray.direction[0],
newray.direction[1],
newray.direction[2],
level+1,time);*/
translucencyray = TRUE;
                                tracecolor = trace(&newray, level,time);
translucencyray = FALSE;
/*printf("%f,%f,%f\n",tracecolor.red,tracecolor.grn,tracecolor.blu);*/
viewcolor.red += tracecolor.red *p->transmittivity;
viewcolor.grn += tracecolor.grn *p->transmittivity;
viewcolor.blu += tracecolor.blu *p->transmittivity;
}
return(viewcolor);
}
pvf2(x)
double x;
{
return((int)(16 *drand()+4080. *(x<0.70.:1.<x?!:x)));
}

double Fn = 0.0;
double focaldistance = 1.0;

struct color eyetrace(x, y, t)
double x, y, t;
{
struct ray ray;
vector screentarget,modeltarget,focaltarget,direction;
double filmplandistance;

/*printf("eyetrace(%f,%f,%f)\n",x,y,t);*/
screentarget[0] = x;
screentarget[1] = y;
screentarget[2] = 1.;
screentarget[3] = 1.;
MxVectorMultiply(screentarget,inversenormalizer,modeltarget);
VxSubtract(modeltarget,viewpoint,direction);
filmplandistance = VxLength(direction);
VxAddLerp(focaldistance/filmplandistance,viewpoint,direction,focaltarget);
{
vector random;
random[2] = 0;
random[3] = 1;
for (;;)
{
random[0] = 2 *drand()-1;
random[1] = 2 *drand()-1;
if (VxLength(random) <= 1) break;
}
VxScalarMultiply(Fn,random,random);
MxVectorMultiply(random,inversenormaliser,ray.endpoint);
}
VxSubtract(focaltarget,ray.endpoint,ray.direction);
return(trace(&ray, 0, t));
}

```

pv12

PFILE pficfile;

```

extern struct xy {float x,y;} Location[];
extern float Times[];
extern float Filter[4][SS][3][3];

```

```

double t0 = 0.0;
double t1 = 1.0;
settime()

```

settime

```

{
t0 = stof(aargv[1]);
t1 = stof(aargv[2]);
}

```

setppfxy()

setppfxy

```

{
ppfx = stoi(aargv[1]);
ppfy = stoi(aargv[2]);
spfx = 1 + (ppfx-1)/ppx;
spfy = 1 + (ppfy-1)/ppy;
}

```

setsize()

setsize

```

{
ssize = stoi(aargv[1]);
ppe = 1 << ssize;
}

```



```

    spfx = 1 + (ppfx-1)/pps;
    spfy = 1 + (ppfy-1)/pps;
    rpp = SS/(pps*pps);
}
struct aarg_cmd cmd[] = {
    0, setppfx,      "-s %d %d", "ppfx ppy", 0,0,0,0,
    0, setssize,    "-ss %d<0,3>|", "ssize: 0, 1, 2, 3", 0,0,0,0,0,
    0, settime,     "-t %f %f", "starttime endtime", 0,0,0,0,
    0, setdebug,   "-d|", "debug", 0,0,0,0,
    0, setystart,  "-y %d %d", "compute sample area %d to %d in y", 0,0,0,0,0,
    0,0,(char *)std_cmd,0,0,0,0,0,
    0,0,0,0,0,0,0
};

```

```

remain(argc, argv)
char *argv[];

```

remain

```

{
    vector viewdirection, updirection, focuspoint, uppoint;
    char sname[128];
    char label[256];
    int x,y;
    register struct light *lptr;
        vector abc;
        matrix MR1, MR2;
    int c;
    struct color pixel[SS];

    yend = MIN(yend, spfy-1);
    sprintf(label, "pray -s %d %d -m %d -t %f %f -y %d %d",
        ppfx, ppy, ssize, t0, t1, ystart, yend);
    PicSetLabel(label);
    PicSetPsizex(ppfx, (yend-ystart+1)*pps);
    PicSetPsize(ppfy, (yend-ystart+1)*pps);
    PicSetPformat(PF_RGBA);
    PicSetPmatting(PK1_MTD);
    PicSetForce(1);
    PicSetOffset(0, ystart*pps);
    if((picfile = PicCreat(argv[1], 0444)) == NULL) {
        fprintf(stderr, "sphere: Can't create %s\n", argv[1]);
        exit(1);
    }
    picPreEncodeScanline(picfile, 0L);
    /*
     * Read some input
     */
    while((c = getchar()) != EOF) switch(c) {
    case '\t': case '\n': break;
    case 'f': do c = getchar(); while(c != '\n' && c != EOF); break;
    case 'f': if (scanf("%f%f", &fieldofview) != 1)
        fprintf(stderr, "invalid field of view\n");
        break;
    case 'v':
        if (scanf("%f%f%f%f%f%f",
            &viewpoint[0], &viewpoint[1], &viewpoint[2],
            &focuspoint[0], &focuspoint[1], &focuspoint[2],
            &uppoint[0], &uppoint[1], &uppoint[2])
            != 9)
            fprintf(stderr, "invalid viewpoint\n");
        else
            {
                uppoint[3] = 1;
                viewpoint[3] = 1;
                focuspoint[3] = 1;
                VxSubtract(focuspoint, viewpoint, viewdirection);
                focaldistance = VxLength(viewdirection);
                VxSubtract(uppoint, viewpoint, updirection);
            }
        break;
    case 'a':
        if (scanf("%f", &ambient) != 1)
            fprintf(stderr, "invalid ambient light\n");
        break;
    case 's':
        {
            double azimuth, pitch, roll;
            if (scanf("%f%f%f%f%f",
                &esphere->center[0], &esphere->center[1], &esphere->center[2],
                &esphere->radius,
                &azimuth, &pitch, &roll,
                &esphere->outsidecolor.red, &esphere->outsidecolor.grn, &esphere->outsidecolor.blu, &esphere->outsidecolor&
                &esphere->stripecolor.red, &esphere->stripecolor.grn, &esphere->stripecolor.blu, &esphere->stripecolor.all,
                &esphere->refractiveindex, &esphere->transmittivity,
                &esphere->specularity, &esphere->phong,
                ...remain
            ) != 16)
                break;
        }
    }
}

```

```

fbname
) (= 20)
else
    sprintf(stderr, "Invalid sphere\n");
else
    {
    double v;
    matrix tempmatrix;
    FbErrors(FBIGNORE);
    if ((esphere->buniptr == FbOpen(fbname)) == NULL)
        {
        sprintf(stderr, "cannot open %s\n", fbname);
        }
    else
        {
        BuniCSRType csr;
        esphere->fbxsize = GetXSize(esphere->buniptr);
        esphere->fbysize = GetYSize(esphere->buniptr);
        /* all */
        csr.ChannelSel = 017;
        csr.AutoIncDec = INCREMENT;
        csr.WriteTrigger = ALPHA_TRIGGER;
        csr.ReadTrigger = RED_TRIGGER;
        csr.XYMod = X_MOD;
        csr.BumpXY = 8;
        csr.WriteAddrMod = 0;
        csr.ReadAddrMod = 0;
        csr.LerpMode = 0;
        csr.LerpRequest = 0;
        SetBuniCSR(esphere->buniptr, csr);
        sprintf(stderr, "%s: %d %d\n", fbname, esphere->fbxsize, esphere->fbysize)
        }
        MxRotate(azimuth, 'x', esphere->M);
        MxRotate(pitch, 'y', tempmatrix);
        MxMultiply(esphere->M, tempmatrix, esphere->M);
        MxRotate(roll, 'z', tempmatrix);
        MxMultiply(esphere->M, tempmatrix, esphere->M);

        esphere->center[3] = 1.;
        esphere->mptr = 0;
        esphere->reflectiondispersion = 0;
        esphere->transmissiondispersion = 0;
        esphere++;
        }
    }
break;
case 'h':
    {
    int spherenumber;
    double starttime;
    if (scanf("%d%lf%lf%lf",
        &spherenumber, &starttime,
        &abc[0], &abc[1], &abc[2]) != 5)
        sprintf(stderr, "Invalid hit\n");
    }
    ...remain

else
    {
    struct movement *oldmptr, *newmptr;
    double v;
    abc[3] = 1.;
    newmptr = (struct movement *) malloc(sizeof(struct movement));
    if (oldmptr == sphere[spherenumber].mptr)
        {
        while (oldmptr->mptr) oldmptr = oldmptr->mptr;
        oldmptr->mptr = newmptr;
        }
    else
        sphere[spherenumber].mptr = newmptr;

    newmptr->mptr = 0;
    newmptr->starttime = starttime;
    VxCopy(abc, newmptr->translate);
    }
}
/*
abc is the translation vector for the moving sphere.
Let us take a perpendicular vector to it in the same s plane
and follow the formulae from page 256 of Newman & Sproull, et
for rotating about an arbitrary vector.
*/
{double temp; temp = abc[0]; abc[0] = abc[1]; abc[1] = -temp;}

VxNormalize(=bc, abc);
v = sqrt((double)(abc[1]*abc[1] + abc[2]*abc[2]));
MxIdentity(MR1);
MR1[1][1] = MR1[2][2] = abc[2]/v ;
MR1[2][1] = -MR1[1][2] = abc[1]/v;
MxIdentity(MR2);
MR2[0][0] = MR2[2][2] = v ;
MR2[2][0] = -MR2[0][2] = abc[0];

```

```

MixMultiply(MR1,MR2,newmptr->MR1MR2);
MR1[2][1] = -MR1[2][1];
MR1[1][2] = -MR1[1][2];
MR2[2][0] = -MR2[2][0];
MR2[0][2] = -MR2[0][2];
MixMultiply(MR2,MR1,newmptr->IR2IR1);
}
break;
case 'l':
if(scanf("%f%f%f%f%f%f%f%f",
&elght->location0[0], &elght->location0[1], &elght->location0[2],
&elght->intensity0,
&elght->location1[0], &elght->location1[1], &elght->location1[2],
&elght->intensity1,
&elght->radius) != 9)
fprintf(stderr, "Invalid light\n");
else
{
elght->location0[3] = 1.;
elght->location1[3] = 1.;
elght->rgb.red =
elght->rgb.grn =
elght->rgb.blu =
elght->rgb.alf = 1.;
elght++;
}
break;
case 'p':
(double dummy;
...remain

if(scanf("%i%i%i%i%i", &dummy, &dummy, &dummy, &dummy) != 4)
fprintf(stderr, "Invalid plane\n");
}
break;
case 'm':
halfstripewidth = halfringwidth = linethickness = 0;
ringradius = 1.01;
break;
case 'c':
if(scanf("%i", &Fn) != 1)
fprintf(stderr, "Invalid camera lens\n");
break;
case 'b':
if(scanf("%d", &dms) != 1)
fprintf(stderr, "Invalid border\n");
break;
default:
fprintf(stderr, "Unrecognised command ");
do
{
putc(c, stderr);
c=getchar();
}
while (c != EOF && c != '\n');
putc('\n', stderr);
printf("%d spheres, %d lights\n", esphere-sphere, elight-light);
/*
for (lptr = light; lptr != elight; lptr++)
{
VsNormalize(lptr->location0, lptr->location0);
VsNormalize(lptr->location1, lptr->location1);
}
*/
allocatecolorlinebuffers();
if (debug)
{
fprintf(stderr, "pps = %3d\n", pps);
fprintf(stderr, "ppfx,ppfy = (%3d,%3d)\n", ppfx,ppfy);
fprintf(stderr, "spfx,spfy = (%3d,%3d)\n", spfx,spfy);
}
/*oldway
CvuCamera(viewpoint,locuopoint,uppoint,0.);
*/
CvuCamera(dblviewpoint,dblviewdirection,dblupdirection,0.);

CvuPerspective(fieldofview,1.333333,0.1,5.0);
CvuGetN(normalizer);
MixInvert(normalizer,inversenormalizer);
CvuViewPrint();
/*
CvuSetScreenWindow(spfx-1.,0.,spfy-1.,0.,255,0.);
*/

```

```

CvuSetScreenWindow(0.,spx-1.,0.,spx-1.,0.,255.);
{
  struct sphere *sptr;
  matrix N,P,S,T;
  CvuGetN(N);

  CvuGetP(P);

  CvuGetS(S);

  for (sptr = sphere; sptr != endhere; sptr++)
  {
    vector center;
    struct window w0,w1;
    FindCenter(sptr,t0,center);
    MxTranslate((double)center[0],
               (double)center[1],
               (double)center[2],T);

    MxMultiply(T,N,T);
    MxMultiply(T,P,T);
    MxMultiply(T,S,T);
    boundsphere(sptr->radius,T,&w0);

    FindCenter(sptr,t1,center);
    MxTranslate((double)center[0],
               (double)center[1],
               (double)center[2],T);

    MxMultiply(T,N,T);
    MxMultiply(T,P,T);
    MxMultiply(T,S,T);
    boundsphere(sptr->radius,T,&w1);

    if (w0.minx > w1.minx) w0.minx = w1.minx;
    if (w0.miny > w1.miny) w0.miny = w1.miny;
    if (w0.maxx < w1.maxx) w0.maxx = w1.maxx;
    if (w0.maxy < w1.maxy) w0.maxy = w1.maxy;

    {
      double duration;
      struct movement *mptr;

      VzCopy(sptr->center,center);
      if (mptr = sptr->mptr)
        while (mptr->mptr)
          {
            if ((t0 < mptr->starttime) && (t1 > mptr->starttime))
              {
                MxTranslate((double)center[0],
                           (double)center[1],
                           (double)center[2],T);

                MxMultiply(T,N,T);
                MxMultiply(T,P,T);
                MxMultiply(T,S,T);
                boundsphere(sptr->radius,T,&w1);

                if (w0.minx > w1.minx) w0.minx = w1.minx;
                if (w0.miny > w1.miny) w0.miny = w1.miny;
                if (w0.maxx < w1.maxx) w0.maxx = w1.maxx;
                if (w0.maxy < w1.maxy) w0.maxy = w1.maxy;
              }

            duration = mptr->mptr->starttime - mptr->starttime;
            VzAddLerp(duration,center,mptr->translate,center);
            mptr = mptr->mptr;
          }

            if ((t0 < mptr->starttime) && (t1 > mptr->starttime))
              {
                MxTranslate((double)center[0],
                           (double)center[1],
                           (double)center[2],T);

                MxMultiply(T,N,T);
                MxMultiply(T,P,T);
                MxMultiply(T,S,T);

                ...remain

                boundsphere(sptr->radius,T,&w1);

                if (w0.minx > w1.minx) w0.minx = w1.minx;
                if (w0.miny > w1.miny) w0.miny = w1.miny;
                if (w0.maxx < w1.maxx) w0.maxx = w1.maxx;
                if (w0.maxy < w1.maxy) w0.maxy = w1.maxy;
              }
          }
    }

    sptr->w = w0;
    printf("%d,%d,%d,%d,%d\n",sptr,sptr->w.minx,sptr->w.maxx,sptr->w.miny,sptr->w.maxy);
    /* Concatenate all of the current matrices that affect the sphere.
     * Let T be the concatenated matrix that transforms the sphere from
  
```

* model space to object space (cmx) to eye space (Noubi) to screen
* space (NcPS).

```

}
}
for (sy = ystart-1; sy <= yend+1; sy++)
{
    if (debug)
        {printf(stderr, "%3d\r", sy); fflush(stdout);}
    cyclecolorlinebuffers();
    if (yactivespheres(sy))
        for (sx = 0; sx <= spfx; sx++)
            if (xyactivespheres(sx, sy))
                {
                    int m;
                    int timeoffset;
                    if (debug)
                        {printf(stderr, "%3d\r", sx); fflush(stdout);}
                    timeoffset = sx*6 + sy*6;
                    for (ss = 0; ss <= SS; ss++)
                        {
                            pixel[ss] = eyetrace(
                                2*(sx+Location[ss].x+drand())/SS)/spfx - 1,
                                1 - 2*(sy+Location[ss].y+drand())/SS)/sply,
                                t0 + (t1-t0)*(Times[(ss+timeoffset)%SS]+drand()/SS));
                        }
                    accumulateSS(pixel, sx*pps);
                }
    if ((sy != ystart-1) && (sy != yend+1))
        writecolorlinebuffers();
}
if (!picPostEncodeScanline(picfile))
    printf("sphere: trouble writing tile in %s\n", argv[1]);
PicClose(picfile);
}

```

RGBAPixelType RGBALine;

```

struct color *colorlineptr;
writecolorlinebuffers()

```

writecolorlinebuffers

```

{
    int i;
    for (i = 0; i < pps; i++)
        {
            converttoRGBALine(colorlineptr[i]+2);
            picEncodeScanline(picfile, RGBALine);
        }
}

```

allocatelinebuffers()

allocatelinebuffers
...allocatelinebuffers

```

{
    int i;
    RGBALine = (RGBAPixelType *)malloc((unsigned)sizeof(RGBAPixelType)*pps);
    colorlineptr = (struct color *)malloc((unsigned)sizeof(struct color)*(pps+2));
    for (i = 0; i < pps+2; i++)
        colorlineptr[i] = (struct color *)malloc((unsigned)sizeof(struct color)*(pps+pps+2));
}

```

cyclecolorlinebuffers()

cyclecolorlinebuffers

```

{
    int i, j;
    struct color *temp0, *templ;
    struct color *colorptr;

    temp0 = colorlineptr[pps];
    templ = colorlineptr[pps+1];
    for (i = pps+1; i >= 2; i--)
        {
            colorptr = colorlineptr[i] = colorlineptr[i-2];
            for (j = pps+pps+2; j > 0; j--)
                *colorptr++ = nullcolor;
        }
    colorlineptr[0] = temp0;
    colorlineptr[1] = templ;
}

```

converttoRGBALine(colorlineptr)
struct color *colorlineptr;

converttoRGBALine

```

{
    RGBAPixelType RGBALineptr;
    int x;
    for (x = 0; RGBALineptr = RGBALine; x < ppx; x++, RGBALineptr++, colorlineptr++)
        {
            RGBALineptr->Red = pv12(colorlineptr->red);
            RGBALineptr->Green = pv12(colorlineptr->grn);
            RGBALineptr->Blue = pv12(colorlineptr->blu);
            RGBALineptr->Alpha = pv12(colorlineptr->alf);
        }
}

```

xyactivespheres(sx, sy)

xyactivespheres

```

struct sphere *p;
int flag;
flag = 0;
for(p=sphere;p != esphere;p++)
    flag |=
    p->active =
    (((sx >= p->w.minx-dms) && (sx <= p->w.maxx+dms)) &&
    ((sy >= p->w.miny-dms) && (sy <= p->w.maxy+dms)));
/*printf("%d:%d\n",p,p->active);*/
return(flag);
}

```

yactivespheres(sy)

yactivespheres

```

struct sphere *p;
int flag;
flag = 0;
for(p=sphere;p != esphere;p++)
    flag |=
    p->active = ((sy >= p->w.miny-dms) && (sy <= p->w.maxy+dms));

```

...yactivespheres

/*printf("%d:%d\n",p,p->active);*/

return(flag);

/*

The active flag indicates that the sphere touches this scanline. This can be answered by intersecting the plane determined by the point of view with the scanline with the sphere. Actually, of course, the plane is 3d, one scanline high; the sphere is 4d, moving as it does through time. A simple approximation to reduce the plane back down to 2d is to intersect it with a sphere larger in radius by one extra scanline. Furthermore, the moving sphere can be neglected by using the average of the two sphere centers, with a radius increased by half the difference.

*/

accumulateSS(pSSptr,x)

accumulateSS

```

struct color *pSSptr;
{
int m;
int i,j,k,l,m;
float *ptr;
float f;
struct color *colorptr;

ss = 0;
for (j = 0; j < pps; j++)
    for (i = 0; i < pps; i++)
        for (k = rpp; k > 0; k--)
            {
int xoffset,yoffset;
fptr = &Filter[ssize][ss][0][0];
xoffset = Location[ss].x*pps;
yoffset = Location[ss].y*pps;
for (m = 0; m < 3; m++)
            {
colorptr = colorlineptr[yoffset+m]+xoffset+x;
for (l = 0; l < 3; l++)
                {
f = *ptr++;
colorptr->red += pSSptr->red*f;
colorptr->grn += pSSptr->grn*f;
colorptr->blu += pSSptr->blu*f;
colorptr->alf += pSSptr->alf*f;
colorptr++;
}
}
}
pSSptr++; ss++;
}
}
}

```

main(argc, argv)

main

```

char *argv[];
{
argc = do_args(cmd,argc,argv);
if (aa_helpflag) exit(0);
if (argc < 2)
    {printf("Usage: gt filename\n");exit(1);}
}

```

...main

remain(argc, argv);

It is claimed:

1. In a method of forming an electronic signal of a video image frame that individually specifies characteristic information of each of an array of pixels that forms said frame, wherein the characteristic information of each pixel is determined by sampling, at a plurality of points within a boundary of each of said pixels, data stored in a computer data base that specifies visual characteristics of an object scene for said image frame, the improvement comprising the steps of electronically determining, for the sample points individually, a range of angles of reflection of the object scene at such points, and pseudo-randomly selecting one such angle for each such sample point, whereby other portions of the object scene that are visible by reflection from a sampled point of the object scene are determined.

2. The method according to claim 1 wherein said improvement additionally comprises the steps of determining, for the sample points individually, a range of angles of rays extending from each such point to a source of illumination of the scene, pseudo-randomly selecting one such ray angle for each such point, and determining for each of said selected rays whether other objects are in the path of the ray, whereby penumbras are shown in the image frame.

3. In a method of forming an electronic signal of a video image frame that individually specifies characteristic information of each of an array of pixels that forms said frame, wherein the characteristic information of each pixel is determined by sampling, at a plurality of points within a boundary of each of said pixels, data stored in a computer data base that specifies visual characteristics of an object scene for said image frame, the improvement comprising the steps of electronically determining, for the sample points individually, a range of angles of rays extending from each such point to a source of illumination of the scene pseudo-randomly selecting one such angle for each such point, and determining for each of said selected rays whether other objects are in its path, whereby penumbras are shown in the image frame.

4. A system for developing an electronic signal and displaying an image of an object scene therefrom, comprising:

a computer memory database that specifies certain static and time varying visual characteristics of the object scene,

means responsive to said computer memory for sampling information of the database to determine the visual characteristics of the object scene at a plurality of points pseudo-randomly positioned across the object scene, and

means responsive to said computer memory for causing said plurality of point samples to be pseudo-randomly distributed in time,

whereby an image is displayed monitor with reduced spatial and temporal aliasing.

5. The system according to claim 4 which additionally comprises means responsive to said computer memory for positioning said sample points in a manner that the resulting displayed image views the object scene as if through an optical system having a limited aperture size and specific focal characteristics.

6. The system according to either of claims 4 or 5 which additionally comprises means responsive to said computer memory for pseudo-randomly selecting for

each sample point one of a range of angles of reflection of the object scene at such points, whereby other portions of the object scene that are visible by reflection a single point of the object scene are determined.

7. The system according to either of claims 4 or 5 which additionally comprises means responsive to said computer memory for determining partial blocking of object scene illumination source, thereby to show penumbras in the displayed image.

8. The system according to either of claims 4 or 5 which additionally comprises means responsive to said computer memory for pseudo-randomly selecting for each sample point one of a range of angles of refraction of the object scene at such points, whereby other portions of the object scene that are visible by transparency through a single point of the object scene are determined.

9. In a method of forming an electronic signal of a video image frame that individually specifies characteristic information of each an array of pixels that form said frame, wherein the characteristic information of each pixel is determined by sampling, at a plurality of points within a boundary of each of said pixels, data stored in a computer data base that specifies visual characteristics of an object scene for said image frame, the improvement comprising the steps of electronically determining, for the sample points individually, a range of angles of refraction of the object scene at such points, and pseudo-randomly selecting one such angle for each such sample point, whereby other portions of the object scene that are visible by transparency through a sample point of the object scene are determined.

10. In a method of forming an electronic signal of a video image frame that individually specifies characteristic information of each of an array of pixels that form said frame, wherein the characteristic information of each pixel is determined by sampling at at least one point within a boundary of each of said pixels, data stored in a computer data base that specifies spatial locations and the visual characteristics of objects in a scene for said image frame, the improvement comprising electronically positioning said sample points in a spatial distribution across said frame such that a Fourier transform of such a distribution over an infinite extent is substantially continuous in some regions and establishing the characteristics of an optical imaging system, including aperture size and focal plane relative to the objects of the scene, and determining the characteristics of the objects for each sample by taking into account the distance of the objects from the focal plane and the size of the lens aperture, whereby the image frame electronic signal contains information of the objects within a certain depth of field as determined by the characteristics of the optical imaging system.

11. The method according to claim 10 wherein said improvement additionally comprises the steps of determining, for the sample points individually, a range of angles of reflection of the object scene at such points, and pseudo-randomly selecting one such angle for each such sample point, whereby other portions of the object scene that are visible by reflection from a sample point of the object scene are determined.

12. The method according to claim 10 wherein said improvement additionally comprises the steps of determining, for the sample points individually, a range of angles of refraction of the object scene at such points, and pseudo-randomly selecting one such angle for each such sample point, whereby other portions of the object

scene that are visible by transparency through a sample point of the object scene are determined.

13. In a method of forming an electronic signal of a video image frame that individually specifies characteristic information of each an array of adjacent areas that forms said frame, wherein the characteristic information of each such array is determined by sampling, at a plurality of points in a certain pattern within a boundary of substantially every area across said image frame, data stored in a computer data base that specifies spatial locations and visual characteristics of an object scene for said image frame, the improvement comprising electronically arranging said plurality of sample points within substantially every such area in a spatial distribution therein such that a Fourier transform of such a distribution over an infinite extent has substantially continuous in some regions, and establishing the characteristics of an optical imaging system, including aperture size and focal plane relative to the objects of the scene, and determining the characteristics of the objects for each sample by taking into account the distance of the objects from the focal plane and the size of the lens aperture, whereby the image frame electronic signal contains information of the objects within a certain depth of field as determined characteristics of the optical imaging system.

14. The method according to claim 13 wherein the step of determining the characteristics of the objects includes pseudo-randomly distributing the path of sample points through said lens aperture.

15. A method for point sampling image data in a computer system for determining characteristic information of pixels comprising said image data, said method comprising the steps of:

- selecting a plurality of sample regions comprising at least a portion of a pixel;
- selecting sample points within said regions such that the distribution of sample points of the smallest sample region is nonperiodic, and;
- combining the characteristic information of the sample points in each pixel, thereby to determine a single characteristic information of each pixel.

16. The method of claim 15 wherein said nonperiodic distribution is repeated in each of said plurality of sample regions.

17. A method for point sampling image data in a computer system for determining characteristic information of pixels comprising said image data, said method comprising the steps of:

- selecting a plurality of sample regions comprising at least a portion of a pixel, and;
- selecting sample points within said regions such that the distribution of sample points of the smallest sample region is nonrectangular and nonrectilinear.

18. A method for point sampling image data in a computer system for determining characteristic information of pixels comprising said image data, said method comprising the steps of:

- defining a sample region comprising at least a portion of said one of said pixels;
- defining a grid pattern wherein a first number of regularly spaced sample point locations are defined in said sample region, and;
- point sampling at a second number of selected sample point locations of said grid pattern, said second number being less than said first number, said selected sample point locations disposed in a nonregular distribution in said grid pattern.

19. In a method of forming an electronic signal of a video image frame that individually specifies characteristic information of each of an array of adjacent areas that form said frame, wherein the characteristic information of such area is determined by sampling at a plurality of points in a certain pattern within a boundary of substantially every such area across said image frame, data stored in a computer data base that specifies spatial locations and visual characteristics of an object scene for said image frame, the improvement comprising the steps of electronically defining a plurality of substantially nonoverlapping portions within such area and then locating each sample point within an individual area portion pursuant to a nonregular distribution.

20. In a method of forming an image frame by individually controlling characteristic information of each pixel in an array of pixels that forms said frame, wherein objects to be included in said image frame are represented by image data stored in a computer data base that specifies spatial locations and visual characteristics of said objects for said image frame, a method of accessing the information of said image data for determining the characteristic information of each pixel, said method comprising the steps of:

- spatially dividing the area of said pixel into a plurality of non-overlapping areas;
- determining a nominal point location within each of said areas in a nonregular pattern;
- determining an offset of each such nominal point within each of said areas for each pixel within said image frame to define an offset point such that a plurality of offset points defines a nonregular distribution;
- determining the characteristic information at each offset point for each pixel of said frame, and;
- combining the characteristic information of said offset point in each pixel, thereby to determine a single characteristic information of each pixel.

21. In a method of forming an electronic signal of a video image frame that individually specifies characteristic information of each of an array of pixels that forms said frame, wherein the characteristic information of each pixel is determined by point sampling at at least one point within a boundary of each of said pixels, data stored in a computer data base that specifies various parameters relating to an object scene, the improvement wherein the sampling is electronically accomplished by a pseudo-random distribution of at least one of said stored parameters such that a Fourier transform of such a distribution over an infinite extent contains substantially continuous regions, said at least one stored parameters including location of objects in the scene relative to the image frame.

22. The improved method according to claim 21 wherein said at least one stored parameter includes an amount that the objects in the scene change during the time represented by said video image frame, whereby object blur of said object scene is represented.

23. The improved method according to claim 21 wherein said at least one stored parameter includes a range of ray paths representative of that created by an optical imaging system, whereby a depth of field of said object scene is represented.

24. The improved method according to claim 21 wherein said at least one stored parameter includes a range of angles of reflection from objects in the scene.

25. The improved method according to claim 21 wherein said at least one stored parameter includes a range of angles of refraction by objects in the scene.

26. The improved method according to claim 21 wherein said at least one stored parameter includes a range of spatial intensity variations of illumination and objects in the scene.

27. In a method of forming an electronic signal of a video image frame that individually specifies characteristic information of each of an array of pixels that forms said frame, wherein the characteristic information of each pixel is determined by sampling at least one point within a boundary of each of said pixels, data stored in a computer data base that specifies spatial locations and visual characteristics of objects in a scene for said image frame, the improvement comprising electronically positioning said sample points in a spatial distribution across said frame such that a Fourier transform of such a distribution of over an infinite plane is substantially continuous in some regions, and said improvement additionally comprises locating a plurality of sample points within each pixel and wherein said computer data base contains information of spatial movement of the objects during a time period represented by said image frame, and further wherein the characteristic information of the objects is determined for each of the plurality of sample points within each pixel at one of a plurality of different instants during said image frame time period, thereby to show any motion blur of the object scene in the resulting image frame electronic signal.

28. The method according to claim 27 wherein said improvement additionally comprises the steps of establishing the characteristics of an optical imaging system, including aperture size and focal plane relative to the objects of the scene, and determining the characteristics of the objects for each sample by taking into account the distance of the objects from the focal plane and the size of the lens aperture, whereby the image frame electronic signal contains information of the objects with a certain depth of field as determined by the characteristics of the optical imaging system.

29. The method according to claim 27 wherein said improvement additionally comprises the steps of determining, for the sample points individually, a range of angles of reflection and/or refraction of the object scene at such points, and pseudo-randomly selecting one such angle for each such sample point, whereby other portions of the object scene that are visible by reflection from or transparency through a sample point of the object scene are determined.

30. The method according to claim 27 wherein said improvement additionally comprises the steps of determining, for the sample points individually, a range of angles of rays extending from each such point to a source of illumination of the scene, pseudo-randomly selecting one such ray angle for each such point, and determining for each of said selected rays whether other objects are in the path of the ray, whereby penumbras are shown in the image frame.

31. In a method of forming an electronic signal of a video image frame that individually specifies characteristic information of each of an array of adjacent areas that forms said frame, wherein the characteristic information of each such area is determined by sampling, at a plurality of points in a certain pattern within a boundary of substantially every such area across said image frame, data stored in a computer data base that specifies spatial locations and visual characteristics of an object

scene for said image frame, the improvement comprising electronically arranging said plurality of sample points within substantially every such area in a spatial distribution therein such that a Fourier transform of such a distribution over an infinite plane is substantially continuous in some regions, wherein said electronic information of spatial movement of the object scene during a time period represented by said image frame, and further wherein the characteristic information of the object is determined for each of the plurality of sample points within each frame area at one of a plurality of different instants during said image frame time period, thereby to show any motion blur of the object scene that occurs during the time period of said image frame.

32. The method according to claim 31, wherein said one of a plurality of different instants of time is pseudo-randomly determined for said sample points.

33. The method according to claim 31, wherein said improvement additionally comprises the steps of establishing the characteristics of an optical imaging system, including aperture size and focal plane relative to the objects of the scene, and determining the characteristics of the objects for each sample by taking into account the distance of the objects from the focal plane and the size of the lens aperture, whereby the image frame electronic signal contains information of the objects with a certain depth of field as determined by the characteristics of the optical imaging system.

34. The method according to claim 33 wherein the step of determining the characteristics of the objects includes pseudo-randomly distributing the path of sample points through said lens aperture.

35. The method according to claim 31 wherein said improvement additionally comprises the steps of determining, for said sample points individually, a range of angles of reflection and/or refraction of the object scene at each point, and pseudo-randomly selecting one such angle for each such sample point, whereby other portions of the object scene that are visible by reflection from or transparency through a sampled point of the object scene are determined.

36. The method according to claim 31 wherein said improvement additionally comprises the steps of determining, for the sample points individually, a range of angles of rays extending from each such point to a source of illumination of the scene, pseudo-randomly selecting one such ray angle for each such point, and determining for each of said selected rays whether other objects are in the path of the ray, whereby penumbras are shown in the image frame.

37. In a method of forming an electronic signal of a video image frame that individually specifies characteristic information of each of an array of pixels that forms said frame, wherein the characteristic information of each pixel is determined by sampling, at a plurality of points within a boundary of each of said pixels, data stored in a computer data base that specifies visual characteristics of an object scene for said image frame, the improvement comprising the steps of including in said computer data base information of changes in the object scene visual characteristics that occur during the time period of said image frame, and electronically sampling the data base at said plurality of points at different instants during said time period, whereby any motion blur of the object scene is included in the resulting image frame electronic signal, wherein the steps of sampling the data base at said plurality of points includes doing so

pseudo-randomly as a function of time for each such pixel and within said time period of said image frame, whereby the image frame signal has reduced aliasing in time.

38. The improved method according to claim 37 wherein the step of sampling the data base at said plurality of points includes the steps of defining an interval of time for taking a sample for each of said plurality of points for said pixel, and pseudo-randomly determining the instant of each such sample within its said defined interval of time, whereby the image frame signal has reduced aliasing in time.

39. The improved method according to claim 38 wherein the intervals of time defined for taking each sample are substantially non-overlapping.

40. The improved method according to claim 38 wherein the intervals of time defined for taking each sample are overlapped in a manner to increase the concentration of samples in the middle of the intervals of time relative to the concentration at their beginning and end.

41. The method according to any of claims 37 and 38, inclusive, wherein said improvement additionally comprises the steps of establishing the characteristics of an optical imaging system, including aperture size and focal plane relative to the objects of the scene, and determining the characteristics of the objects for each sample by taking into account the distance of the objects from the focal plane and the size of the lens aperture, whereby the image frame electronic signal contains information of the objects with a certain depth of field as determined by the characteristics of the optical imaging system.

42. The method according to any of claims 37 and 38, inclusive, wherein said improvement additionally comprises the steps of determining, for the sample points individually, a range of angles of reflection and/or refraction of the object scene at such points, and pseudo-randomly selecting one such angle for each such sample point, whereby other portions of the object scene that are visible by reflection from or transparency through a sampled point of the object scene are determined.

43. The method according to any of claims 37 and 38, inclusive, wherein said improvement additionally comprises the steps of determining, for the sample points individually, a range of angles of rays extending from each such point to a source of illumination of the scene, pseudo-randomly selecting one such ray angle for each such point, and determining for each of said selected rays whether other objects are in the path of the ray, whereby penumbras are shown in the image frame.

44. In a method of forming an electronic signal of a video image frame that individually specifies characteristic information of each of an array of pixels that forms said frame, wherein the characteristic information of each pixel is determined by sampling, at a plurality of points within a boundary of each of said pixels, data stored in a computer data base that specifies visual characteristics of an object scene for said image frame, the improvement comprising the steps of establishing the characteristics of an optical imaging system, including aperture size and focal plane relative to the objects of the scene, and electronically determining the visual characteristics of the object scene at each point sample by taking into account the distance of the objects from the focal plane and the size of the lens aperture, whereby the image frame electronic signal contains information of the objects with a certain depth of field

as determined by the characteristics of the optical imaging system, wherein the step of determining the visual characteristics of the object scene for each point sample includes pseudo-randomly determining the point on the lens from which the object scene is sampled within a field of view of the object scene that is determined by the lens aperture and location of the focal plane.

45. The method according to claim 44, wherein said improvement additionally comprises the steps of determining, for the sample points individually, a range of angles of reflection and/or refraction of the object scene at such points, and pseudo-randomly selecting one such angle for each such sample point, whereby other portions of the object scene that are visible by reflection from or transparency through a sampled point of the object scene are determined.

46. The method according to claim 44, wherein said improvement additionally comprises the steps of determining, for the sample points individually, a range of angles or rays extending from each such point to a source of illumination of the scene, pseudo-randomly selecting one such ray angle for each such point, and determining for each of said selected rays whether other objects are in the path of the ray, whereby penumbras are shown in the image frame.

47. The method according to claims 27, 31, 37, 38 or 44 wherein said improvement additionally comprises the steps of determining, for the sample point individually, a range of angles of refraction of the object scene at such points, and pseudo-randomly selecting one such angle for each such sample point, whereby other portions of the object scene that are visible by transparency through a sample point of the object scene are determined.

48. In a method of forming an image frame by individually controlling characteristic information of each pixel in an array of pixels that forms said frame, wherein objects to be included in said image frame are represented by data stored in computer data base that specifies spatial locations and visual characteristics of said objects for said image frame, a method of accessing the information of the computer data base for determining the characteristic information of each pixel, comprising performance of the following steps electronically:

spatially dividing the area of said pixel into a plurality of non-overlapping areas,

pseudo-randomly positioning a sample point within substantially each of said areas, thereby to determine the position of a plurality of sample points for each pixel,

determining from the computer data base the characteristic information of the closest of said objects at each of the plurality of sample points for each pixel of said frame, and

combining the characteristic information of the samples in each pixel, thereby to determine a single characteristic information of each pixel; wherein information of any movement of said objects during the time period of said image frame is included in said computer data base, and wherein the step of determining characteristic information for each offset point comprises the steps of pseudo-randomly assigning each of said sample points to one of a plurality of different times during the image frame time period, and determining object characteristic information for each sample point at its said assigned time, whereby said image will include any

motion blur that occurs during the time period of said image frame.

49. The method according to claim 48, wherein said determining step includes a method comprising the steps of establishing the characteristics of an optical imaging system, including aperture size and focal plane relative to the objects of the scene, and determining the characteristics of the objects for each sample by taking into account the distance of the objects from the focal plane and the size of the lens aperture, whereby the image frame electronic signal contains information of the objects with a certain depth of field as determined by the characteristics of the optical imaging system.

50. The method according to claim 48, wherein said determining step includes a method comprising the steps of determining, for said sample points individually, a range of angles of reflection and/or refraction of the object scene at each point, and pseudo-randomly selecting one such angle for each such sample point, whereby other portions of the object scene that are visible by reflection from or transparency through a sample point of the object scene are determined.

51. The method according to claim 48 wherein said improvement additionally comprises the steps of determining, for the sample points individually, a range of angles of rays extending from each such point to a source of illumination of the scene, pseudo-randomly selecting one such ray angle for each such point, and determining for each of said selected rays whether other objects are in the path of the ray, whereby penumbras are shown in the image frame.

52. In a method of forming an image frame by individually controlling characteristic information of each pixel in an array of pixels that forms said frame, wherein objects to be included in said image frame are represented by data stored in a computer data base that specifies spatial locations and visual characteristics of said objects for said image frame, a method of accessing the information of the computer data base for determining the characteristic information of each pixel, comprising performance of the following steps electronically:

- spatially dividing the area of said pixel into a plurality of non-overlapping areas,
- determining a nominal point location within each of said areas in a non-regular pattern,
- pseudo-randomly determining an offset of each such nominal point within each of said areas for each pixel within said image frame,
- determining from the computer data base the characteristic information of the closest of said objects at each pseudo random offset point for each pixel of said frame, and;

combining the characteristic information of the sample points in each pixel, thereby to determine a single characteristic information of each pixel, wherein information of any movement of said objects during the time period of said image frame is

included in said computer data base, and wherein the step of determining characteristic information for each offset point comprises the steps of pseudo-randomly assigning each of said sample points to one of a plurality of different times during the image frame time period, and determining object characteristic information for each sample point at its said assigned time, whereby said image will include any motion blur that occurs during the time period of said image frame.

53. In a method of forming an image frame by individually controlling characteristic information of each pixel in an array of pixels that forms said frame, wherein objects to be included in said image frame are represented by data stored in a computer data base that specifies spatial locations and visual characteristics of said objects for said image frame, a method of accessing the information of the computer data base for determining the characteristic information of each pixel, comprising performing the following steps electronically:

- spatially dividing the area of said pixel into a plurality of non-overlapping areas,
- determining a nominal point location in substantially the center of each of said areas,
- pseudo-randomly determining an offset of each nominal point within each of said areas for each pixel within said image frame,
- determining from the computer data base the characteristic information of the closest of said objects at each pseudo random offset point for each pixel of said frame, and;

combining the characteristic information of each offset point in each pixel, thereby to determine a single characteristic information of each pixel, wherein information of any movement of said objects during the time period of said image frame is included in said computer data base, and wherein the step of determining characteristic information for each offset point comprises the steps of pseudo-randomly assigning each said offset point to one of a plurality of different times during the image frame time period, and determining object characteristic information for each offset point at its said assigned time, whereby said image will include any motion blur that occurs during the time period of said image frame.

54. The method according to any of claims 48, 52 or 53, inclusive, wherein said determining step includes a method comprising the steps of determining, for said sample points individually, a range of angles of refraction of the object scene at each point, and pseudo-randomly selecting one such angle for each such sample point, whereby other portions of the object scene that are visible by transparency through a sample point of the object scene are determined.

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UNITED STATES PATENT AND TRADEMARK OFFICE
Certificate

Patent No. 4,897,806

Patented: January 30, 1990

On petition requesting issuance of a certificate for correction of inventorship pursuant to 35 U.S.C. 256, it has been found that the above identified patent, through error and without any deceptive intent, improperly sets forth the inventorship.

Accordingly, it is hereby certified that the correct inventorship of this patent is: Robert L. Cook, San Anselmo, CA; Thomas K. Porter, Fairfax, CA; Loren C. Carpenter, Novato, CA; and Rodney Stock, Novato, CA.

Signed and Sealed this Eleventh Day of November 2003.

HEATHER R. HERNDON
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